
“Incremental” Hashing

Reading:

- None in your text.
- Optional reading: ch 12 of *File Structures: An Object-Oriented Approach with C++*, by Folk et al.

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A Problem

Performance degrades if the file becomes heavily loaded,
i.e., if $\frac{\text{actual-number-of-recs}}{\text{num-buckets} \times \text{bucket-size}}$ gets large.

To make things better, it may be worthwhile to increase the number of buckets (and reorganize the data).

This general idea is called **incremental hashing**.

Guess what? There are many ways to do it.

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Incremental Hashing

General Approach

As records are inserted, if performance becomes too low, grow the file.

- *I.e.*, “split” one bucket and disperse its records; some stay put and others go to a new bucket.
- This reduces overflow (collisions to full buckets) and hence reduces the # of file accesses during search.

As records are deleted, if space usage becomes too poor, shrink the file.

- *I.e.*, merge two buckets into one.
- This reduces the total # of buckets, and hence reduces waste.

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File growth and shrinkage is incremental, *i.e.*:

- It happens on the fly.
We do it during insertions and deletions, if needed.
- It happens in small amounts.
We split one bucket rather than rehashing the whole file.

Possible measures of performance include:

- load factor
- average # of disk accesses per search.

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Method I: Linear Hashing

Method

- When performance becomes too poor, split bucket 0. (Yes, this is arbitrary.)
- Split it by doubling the mod factor and re-hashing its contents. *E.g.*,
 $h(k) = k \bmod 3$ becomes
 $h(k) = k \bmod 6$.
- Next time, split bucket 1, then 2, etc.
- Keep a counter to remember which buckets have been split.
 Unsplit ones use the old hash function.
 Split ones use the new.

Merging is analogous but opposite.

# buckets	old	new
hash fcn	$T : 0 \dots (T - 1)$	$T + 1 : 0 \dots T$
	$h(k) = k \bmod 3$	$h(k) = k \bmod 6$
	$h(k) = k \bmod T$	$h(k) = k \bmod 2T$

Guarantee: Every element of bucket 0 will either stay put, or land in the new bucket T .

More generally, if we split bucket b , every record will either stay put, or land in the new bucket $T + b$.

Let k be the record's key.

If it was in bucket b originally, we know
 $k \bmod T = b$.

So k must have been one of these:

$$h \quad T + b \quad 2T + b \quad 3T + b \quad 4T + b \quad 5T + b \quad \dots$$

So when we hash k with the new hash function $h(k) = k \bmod 2T$, we get either:

- b , in which case the record stays put, or
- $T + b$, in which case it goes to the new bucket, $T + b$.

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Questions

Will linear hashing work if we use open addressing to solve collisions?

Why split the “next” bucket? Why not the culprit, *i.e.*, the one we inserted to when we passed the performance threshold?

Decision: What if the split fails, *i.e.*, everything happens to stay put? We could split again.

What happens when we’ve split all the original buckets?

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Method II: Extendible Hashing

Build a dynamic directory (in memory for speed) that copes with the varying load factor.

- Hash function takes you to a *directory* entry, rather than directly to a bucket.
- Because buckets are pointed to, needn't be consecutive in the file. So can add and remove buckets as desired.
- Directory must grow and shrink with number of buckets.
- So # of places to hash to changes. Cope by using only the first so many bits of $h(\text{key})$; change this as necessary to change size of directory.
- If using d bits, directory size is 2^d .
- So have capacity for 2^d buckets, but can start with fewer; even just one.

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How to “grow” the file

When a bucket overflows:

- Split the one bucket in two.
- Half of the directory entries that pointed to the old bucket will still do so, and half will point to the new bucket.

Eventually, we may reach a point where we can't split a bucket this way.

- This occurs when only one directory entry points to the bucket we want to split.
- Then we double the directory size, and re-organize.

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