

# natural language computing

CSC401/2511 – Natural Language Computing – Spring 2019



# This lecture

- An extractive summary of the course.
- Open office hours 15 April 9h30-11h30 (at Vector)



# Exam

- 23 April from 14h00—17h00.

| A-K  | L-ZZ  |
|--|---|
| EX 310   | MS 2158   |
| Exam Centre<br>255 McCaul Street<br> | Medical Sciences<br>1 King's College Circ<br> |

*May be  
subject  
to change*

- **No aids allowed** – your desk should have nothing but:
  - Your UofT ID,
  - The exam, and
  - A writing implement.

# Structure

- Following the format of previous years:
  - 20 **multiple-choice** questions [40 marks]
    - 4 options each.
  - 10 **short-answer** questions [30 marks]
    - Some of these involve simply giving a definition. Others involve some calculation.
  - 3 **subject-specific** questions [30 marks]
    - These questions involve a small component of original thinking.



8. Melamed's method of sentence alignment works by ...
- (a) minimizing the costs of alignments according to the lengths of the aligned sentences.
  - (b) minimizing the costs of alignments according to the lengths of the aligned words.
  - (c) estimating cognates based on 4-graphs.
  - (d) estimating cognates based on longest common subsequences.
9. Greedy decoding in statistical machine translation iteratively updates the best guess of the English translation  $E^*$ , given the French sentence  $F$ , according to ...
- (a) transformations of words and alignments.
  - (b) transformations of words only.
  - (c) the total cost of alignment.
  - (d) the total number of matching cognates.
10. Which of these phonemes is **not** voiced?
- (a) /b/.
  - (b) /ih/.
  - (c) /m/.
  - (d) /k/.
11. The Nyquist rate is ...
- (a) the rate at which the glottis vibrates.
  - (b) twice the rate at which the glottis vibrates.
  - (c) twice the maximum frequency preserved in a sampled signal.
  - (d) twice the sampling rate of a sampled signal.
12. Which feature is known to correlate positively with a sentence's selection into an extractive text summary in the news domain?
- (a) Early position in the document being summarized.
  - (b) High function-word to content-word ratio.
  - (c) High number of stigma words.
  - (d) None of the above.

# Short answer

2. State Bayes's Rule.

3. Name and define the three types of text-to-speech synthesis architectures. Give one advantage each architecture has over the others.

# We can work it out

## SMT 2. (5 marks)

Given the two reference translations below, compute the BLEU score for each of the two candidate translations, assuming that you only consider unigrams and bigrams, and that there is no cap. *Hint:* Your results should be of the form  $x^y$  where  $x$  is a fraction or some other term, and  $y$  is a positive or negative fraction.

**Reference 1** Use the Force Luke

**Reference 2** Use some Force Luke

**Candidate 1** Use some of the Force

**Candidate 2** Use the Force



# Hints for studying

- **Definitions:** *n.pl.* Terms that are useful to know.

- Highlights are also useful to know.

- Not all definitions/highlights are in the exam.
- Not all things on the exam have been highlighted.
  - This review lecture is likewise not a substitute for the rest of the material in this course.

# Hints for studying

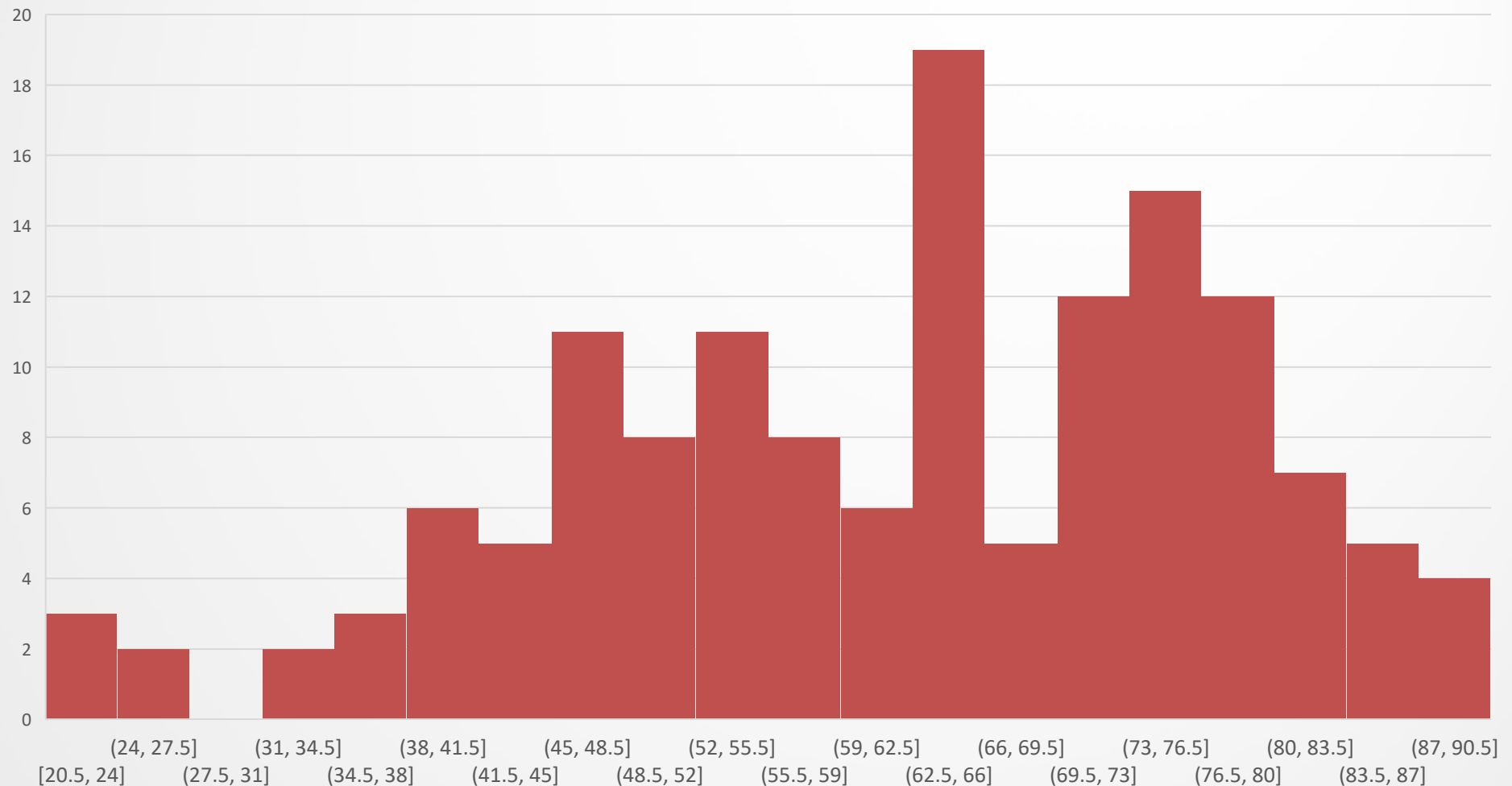
- Go through the **quiz** from this year.
- Work out **worked-out examples** for yourself, ideally more than once.
- I find it helpful to **relax** before an exam.
  - Maybe relax in ways that were also legal  $\geq 1$  year ago.

# Exam material


- The exam covers all material in the lectures and assignments **except**:
  - Material in the bonuses of assignments, and
  - Slides with 'Aside' in the title.
- The reading material (e.g., Manning & Schütze) provides background to concepts discussed in class.
  - If a concept appears in a linked paper but not in the lectures/assignments, you don't need to know it, even if it's **very interesting**.



# 2018 Final exam distribution



# Categories of linguistic knowledge

- Phonology: the study of patterns of speech sounds.  
e.g., “read” → /r i y d/
- Morphology: how words can be changed by inflection or derivation.  
e.g., “read”, “reads”, “reader”, “reading”, ...
- Syntax: the ordering and structure between words and phrases.  
e.g., *NounPhrase* → *det. adj. n.*
- Semantics: the study of how meaning is created by words and phrases.  
e.g., “book” → 
- Pragmatics: the study of meaning in broad contexts.

# Corpora

- **Corpus**: *n.* A body of language data of a particular sort (*pl.* **corpora**).
- Most **valuable** corpora occur **naturally**
  - e.g., newspaper articles, telephone conversations, multilingual transcripts of the United Nations
- We use corpora to gather statistics; more is better (typically between  $10^7$  and  $10^{12}$  tokens).



# Notable corpora

- **Brown corpus**: 1M tokens, 61805 types. Balanced collection of genres in US English from 1961.
- **Penn treebank**: Syntactically annotated Brown, plus others incl. 1989 *Wall Street Journal*.
- **Switchboard corpus**: 120 hours  $\approx$  2.4M tokens. 2.4K telephone conversations between US English speakers.
- **Hansard corpus**: Canadian parliamentary proceedings, French/English bilingual.

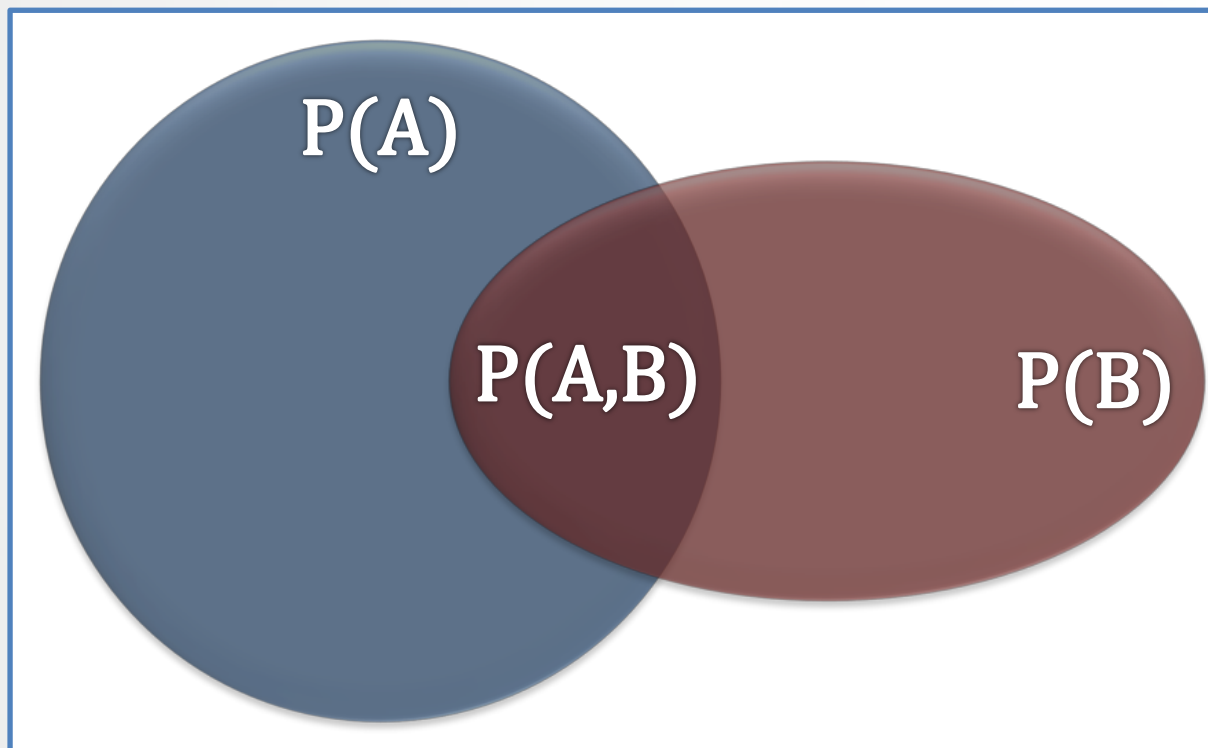
# Very simple predictions

- A model at the heart of SMT, ASR, and IR...
- We want to know the probability of the **next** word given the **previous** words in a sequence.

- We can **approximate** conditional probabilities by counting occurrences in large corpora of data.

- E.g., 
$$P(\textit{food} \mid I \textit{ want Chinese}) = \frac{P(I \textit{ want Chinese food})}{P(I \textit{ want Chinese})} \approx \frac{\textit{Count}(I \textit{ want Chinese food})}{\textit{Count}(I \textit{ want Chinese})}$$

# Bayes' theorem



$$P(A, B) = P(A)P(B|A)$$
$$P(A, B) = P(B)P(A|B)$$

$$\text{Bayes theorem: } P(A|B) = \frac{P(B|A) P(A)}{P(B)}$$



# Maximum likelihood estimate

- **Maximum likelihood estimate (MLE)** of parameters  $\theta$  in a **model**  $M$ , given **training data**  $T$  is

the estimate that maximizes the likelihood of the *training data* using the *model*.

- e.g.,
  - $T$  is the Brown corpus,
  - $M$  is the bigram and unigram tables
  - $\theta_{(to|want)}$  is  $P(to|want)$ .

# Sparsity of unigrams vs. bigrams

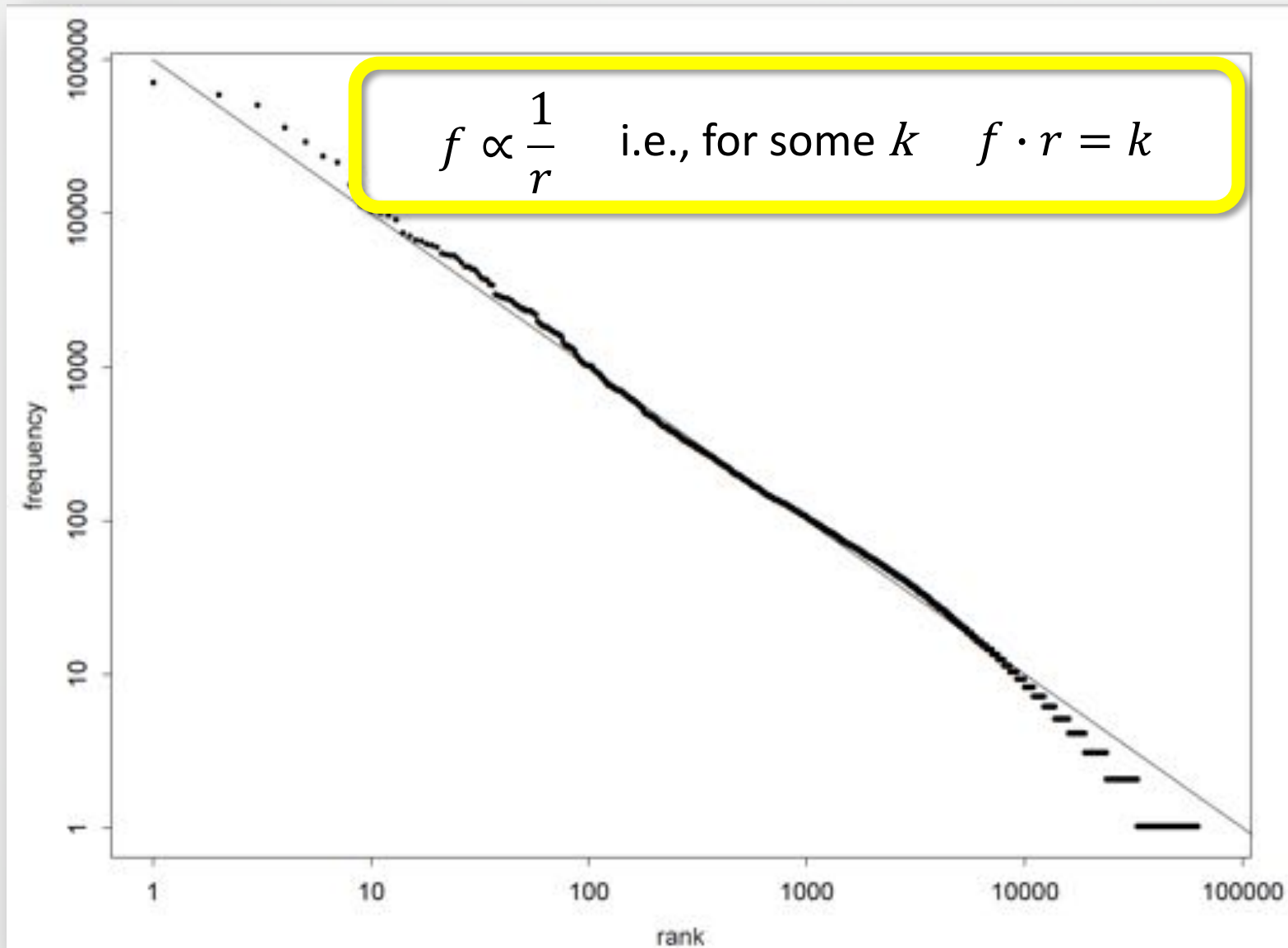
- E.g., we've seen lots of every unigram, but are missing many bigrams:

Unigram counts:

| I    | want | to   | eat | Chinese | food | lunch | spend |
|------|------|------|-----|---------|------|-------|-------|
| 2533 | 927  | 2417 | 746 | 158     | 1093 | 341   | 278   |

| $Count(w_{t-1}, w_t)$ |         | $w_t$ |      |     |     |         |      |       |       |
|-----------------------|---------|-------|------|-----|-----|---------|------|-------|-------|
|                       |         | I     | want | to  | eat | Chinese | food | lunch | spend |
| $w_{t-1}$             | I       | 5     | 827  | 0   | 9   | 0       | 0    | 0     | 2     |
|                       | want    | 2     | 0    | 608 | 1   | 6       | 6    | 5     | 1     |
|                       | to      | 2     | 0    | 4   | 686 | 2       | 0    | 6     | 211   |
|                       | eat     | 0     | 0    | 2   | 0   | 16      | 2    | 42    | 0     |
|                       | Chinese | 1     | 0    | 0   | 0   | 0       | 82   | 1     | 0     |
|                       | food    | 15    | 0    | 15  | 0   | 1       | 4    | 0     | 0     |
|                       | lunch   | 2     | 0    | 0   | 0   | 0       | 1    | 0     | 0     |
|                       | spend   | 1     | 0    | 1   | 0   | 0       | 0    | 0     | 0     |

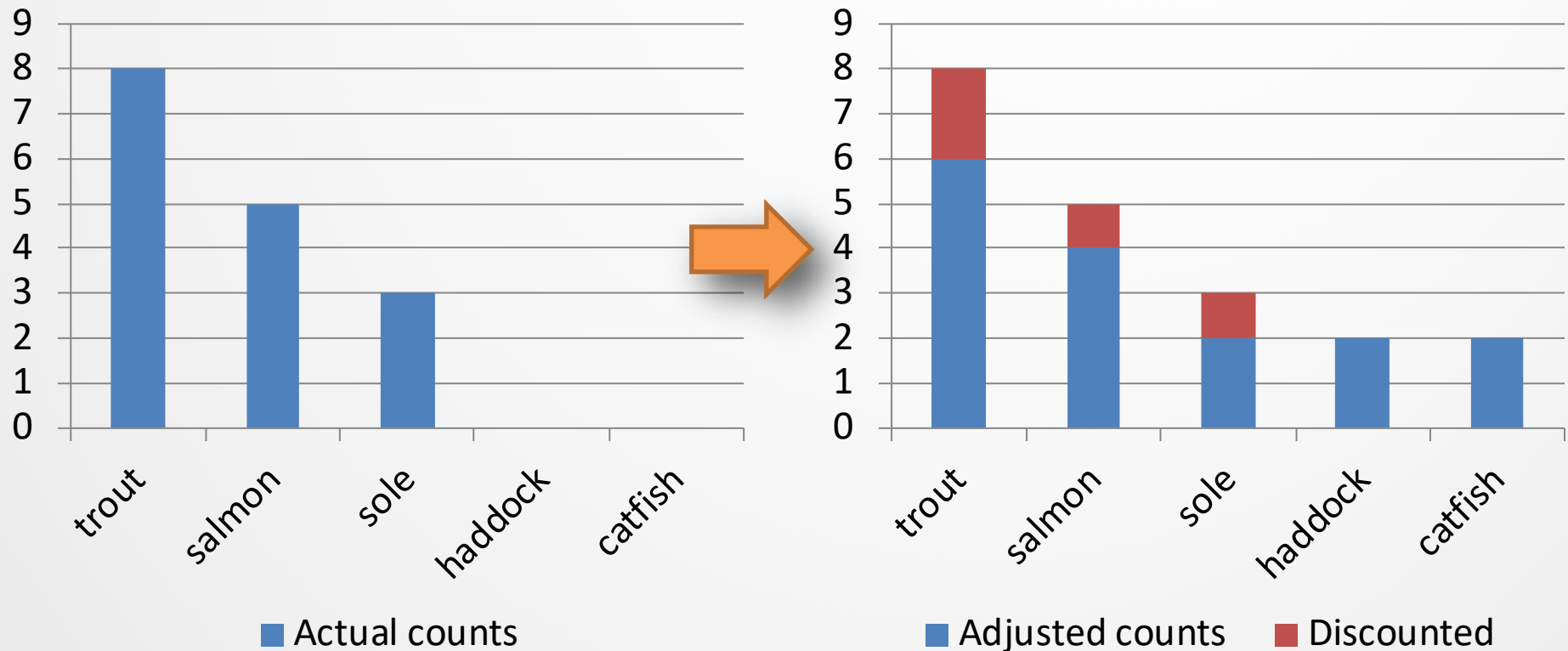
# Zipf's law on the Brown corpus



From Manning & Schütze

# Smoothing as redistribution

- Steal from the rich and give to the poor.
- E.g.,  $\text{Count}(I \text{ caught } \cdot)$



# Add-1 smoothing (Laplace)

- Given a vocab size  $\|\mathcal{V}\|$  and corpus size  $N$ , just add 1 to all the counts! No more zeros!
- MLE :  $P(w_i) = C(w_i)/N$
- Laplace estimate :  $P_{Lap}(w_i) = \frac{C(w_i)+1}{N+\|\mathcal{V}\|}$
- Does this give a proper probability distribution? Yes:

$$\sum_w P_{Lap}(w) = \sum_w \frac{C(w) + 1}{N + \|\mathcal{V}\|} = \frac{\sum_w C(w) + \sum_w 1}{N + \|\mathcal{V}\|} = \frac{N + \|\mathcal{V}\|}{N + \|\mathcal{V}\|} = 1$$



# Add- $\delta$ smoothing

- Laplace's method generalizes to the add- $\delta$  estimate :

$$P_{\delta}(w_i) = \frac{C(w_i) + \delta}{N + \delta||\mathcal{V}||}$$

- Consider also:
  - Simple interpolation
  - Katz smoothing
  - Good-Turing smoothing

# Parts of speech (PoS)

- Linguists like to group words according to their **structural function** in building sentences.
  - This is similar to grouping Lego by their shapes.
- **Part-of-speech:** *n.* lexical category or morphological class.

Nouns collectively constitute a part of speech  
(called *Noun*)

# Parts of speech (PoS)

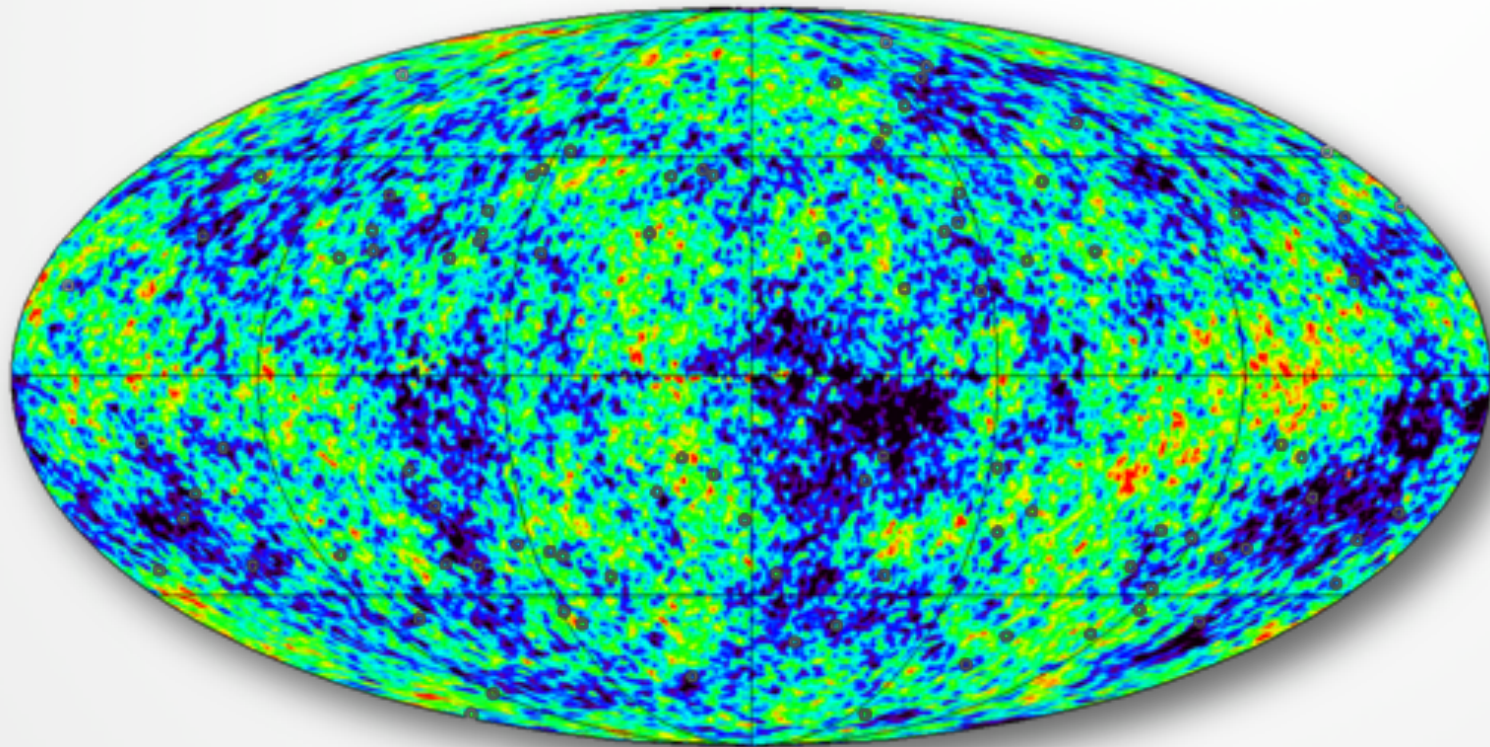
- Things that are useful to know about PoS:
  - **Content words** vs. **function words**
  - **Properties** of content words (e.g., number).
  - **Agreement**. Verbs and nouns should match in *number* in English (e.g., “*the dogs runs*” is ‘wrong’.)
  - What **PoS Tagging** is, and perhaps some vague idea of how to do it.

# mRMR feature selection

- **Minimum-redundancy-maximum-relevance (mRMR)** can use **correlation**, **distance** scores (e.g.,  $D_{KL}$ ) or **mutual information** to select features as in
- For feature set  $S$  of features  $f_i$ , class  $c$ ,  
 $D(S, c)$  : a measure of **relevance** of  $S$  for  $c$ , and  
 $R(S)$  : a measure of the **redundancy** of  $S$ ,

$$S_{mRMR} = \operatorname{argmax}_S [D(S, c) - R(S)]$$

# Information and entropy





# Entropy

- **Entropy:** *n.* the **average** amount of information we get in observing the output of source  $S$ .

$$H(S) = \sum_i p_i I(w_i) = \sum_i p_i \log_2 \frac{1}{p_i}$$

ENTROPY

Note that this is **very** similar to how we define the expected value (i.e., ‘average’) of something:

$$E[X] = \sum_{x \in X} p(x) x$$

# Joint entropy

- **Joint Entropy:** *n.* the **average** amount of information needed to specify multiple variables simultaneously.

$$H(X, Y) = \sum_x \sum_y p(x, y) \log_2 \frac{1}{p(x, y)}$$

Same general form as entropy, except you sum over each variable, and probabilities are joint

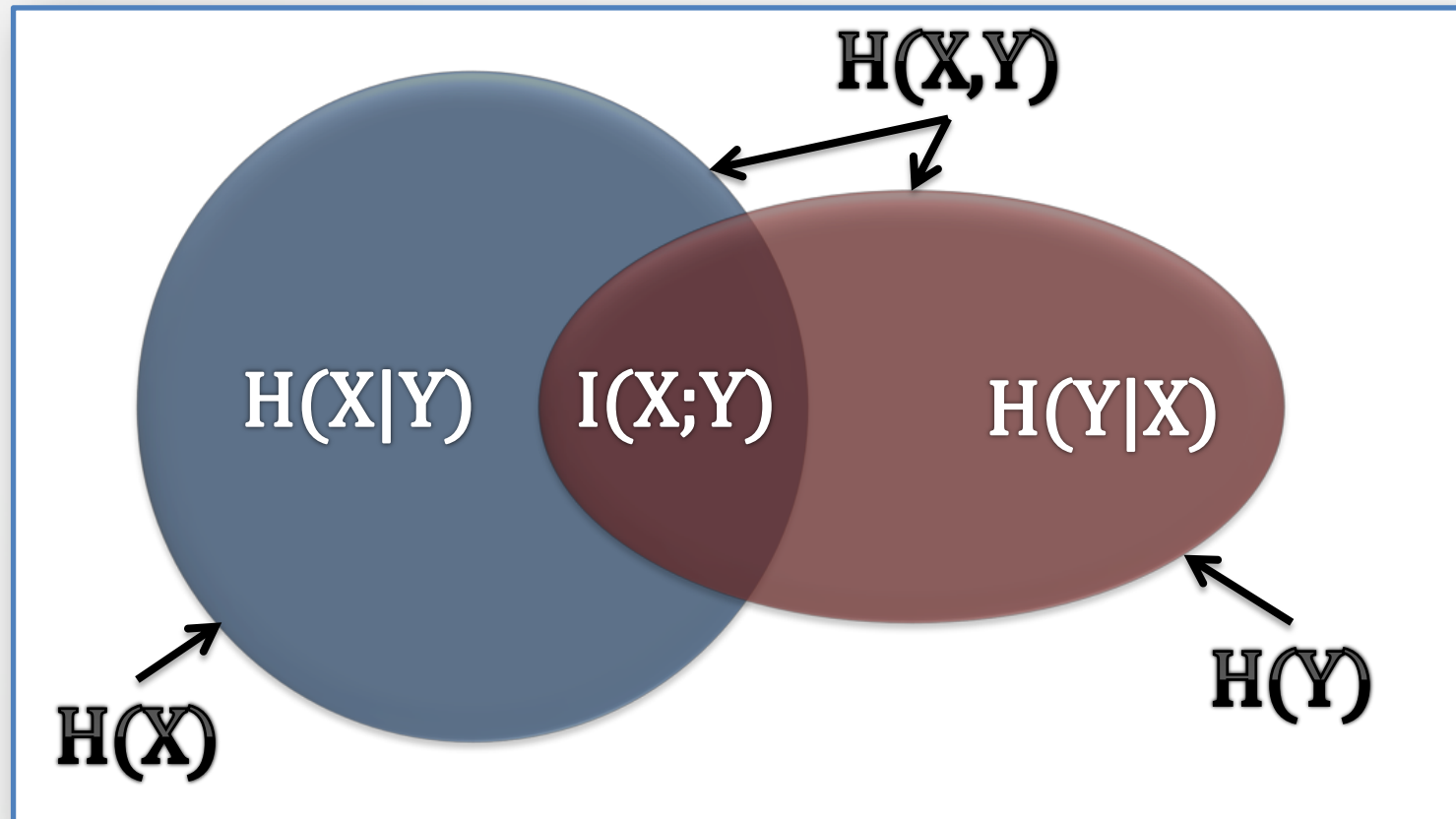
# Conditional entropy

- **Conditional entropy:** *n.* the **average** amount of information needed to specify one variable **given that you know another**.

$$H(Y|X) = \sum_{x \in X} p(x) H(Y|X = x)$$

It's an **average of entropies** over all possible conditioning values.

# Relations between entropies



$$H(X, Y) = H(X) + H(Y) - I(X; Y)$$

# Mutual information

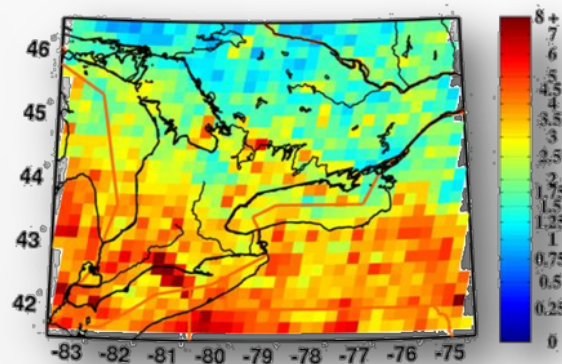
- **Mutual information:** *n.* the **average** amount of information shared between variables.

$$\begin{aligned} I(X; Y) &= H(X) - H(X|Y) = H(Y) - H(Y|X) \\ &= \sum_{x,y} p(x, y) \log_2 \frac{p(x, y)}{p(x)p(y)} \end{aligned}$$

Again, a sum over each variable, but the log fraction is normalized by an assumption that they're independent ( $p(x)p(y)$ ).

# Information theory

- In general, lecture 3 includes some walked-through examples of applying the preceding formula.
  - It's probably a good idea to walk through these examples yourself on paper.



# Collocations

- **Collocation:** *n.* a ‘turn-of-phrase’ or usage where a sequence of words is **perceived** to have a meaning ‘**beyond**’ the sum of its parts.
- E.g., ‘*disk drive*’, ‘*video recorder*’, and ‘*soft drink*’ are collocations. ‘*cylinder drive*’, ‘*video measurer*’, ‘*weak drink*’ are **not** despite some near-synonymy between alternatives.
- Collocations are **not** just highly frequent bigrams, otherwise ‘*of the*’, and ‘*and the*’ would be collocations.
- *How can we test if a bigram is a collocation or not?*

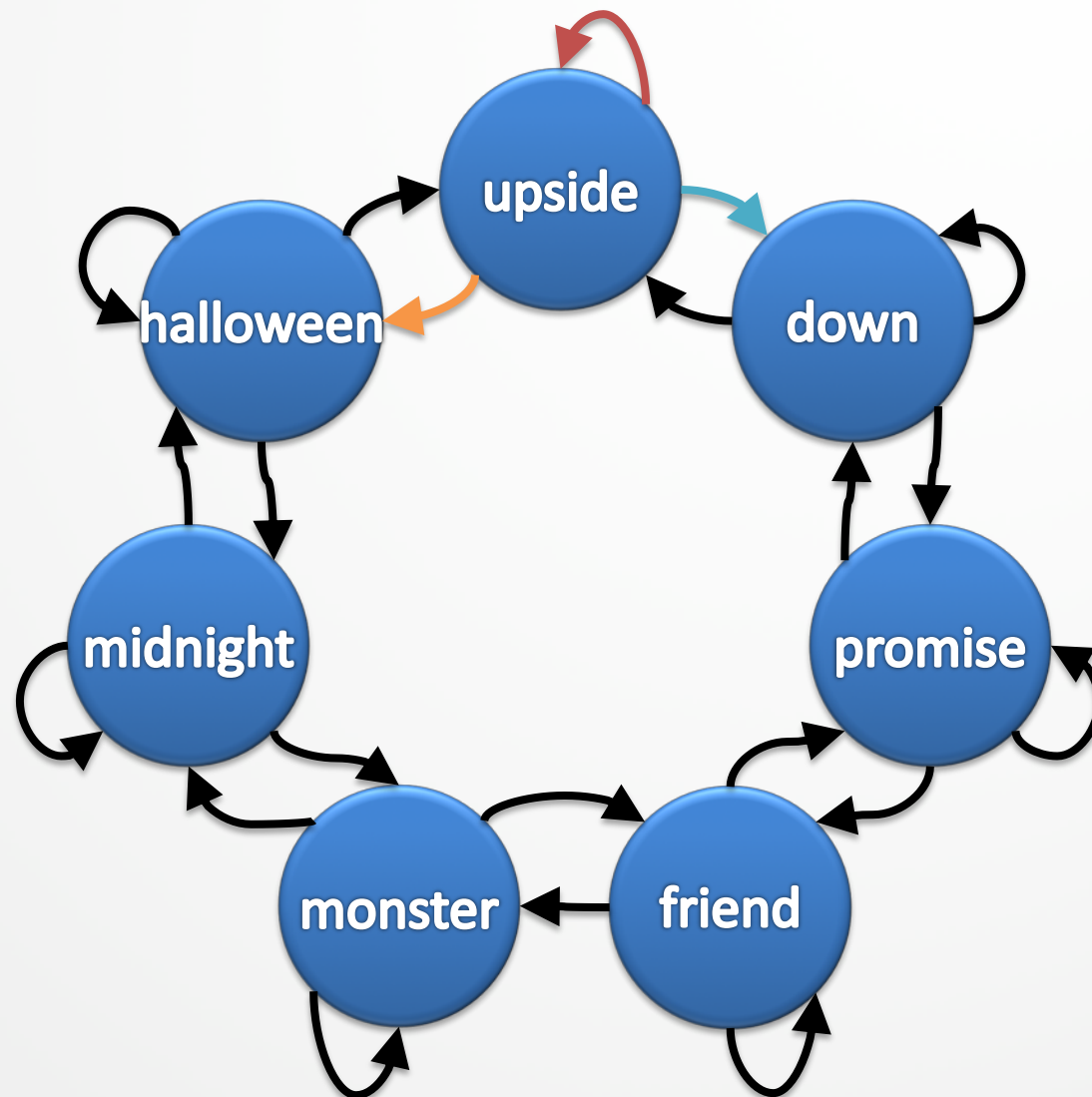


# Decision trees

- Consists of **rules** for classifying data that consists of many **attributes/features**.
- Walk through the DC hero/villain example, lecture 4.



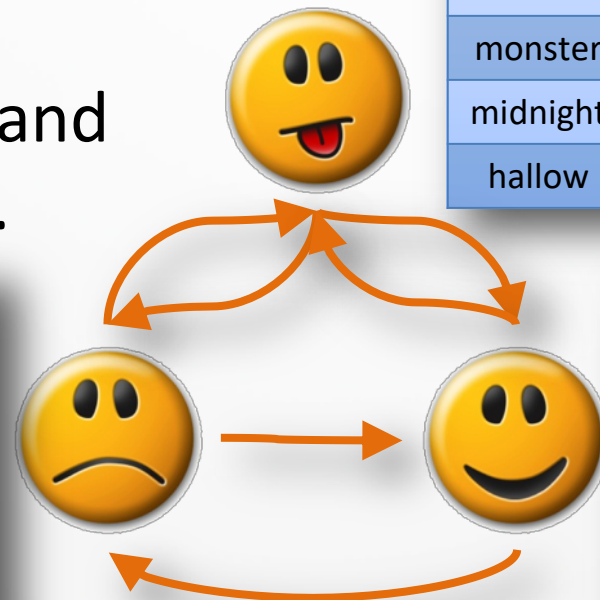
# Observable Markov model



# Multivariate systems

- What if a conditioning variable changes over time?
  - e.g., I'm **happy** one second and **disgusted** the next.
- Here, the **state** is the mood and the **observation** is the word.

| word     | P(word) |
|----------|---------|
| upside   | 0.25    |
| down     | 0.25    |
| promise  | 0.05    |
| friend   | 0.3     |
| monster  | 0.05    |
| midnight | 0.09    |
| hallow   | 0.01    |



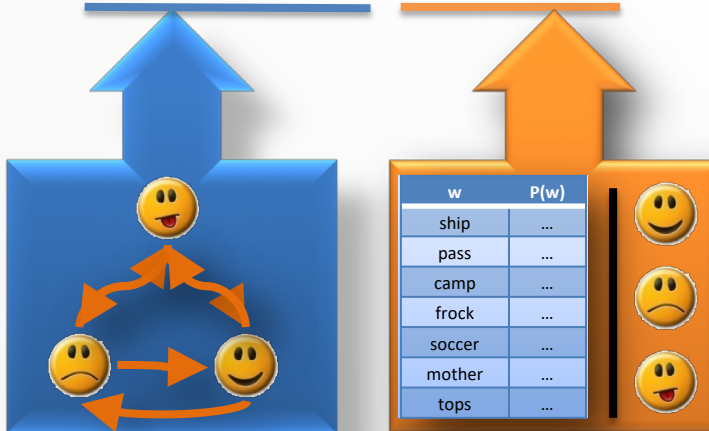
| word     | P(word) |
|----------|---------|
| upside   | 0.1     |
| down     | 0.05    |
| promise  | 0.05    |
| friend   | 0.6     |
| monster  | 0.05    |
| midnight | 0.1     |
| hallow   | 0.05    |

| word     | P(word) |
|----------|---------|
| upside   | 0.3     |
| down     | 0       |
| promise  | 0       |
| friend   | 0.2     |
| monster  | 0.05    |
| midnight | 0.05    |
| hallow   | 0.4     |

# Observable multivariate systems

- Q: How do you **learn** these probabilities?

- $P(w_{0:t}, q_{0:t}) \approx \prod_{i=0}^t \underbrace{P(q_i|q_{i-1})}_{\text{blue}} \underbrace{P(w_i|q_i)}_{\text{orange}}$

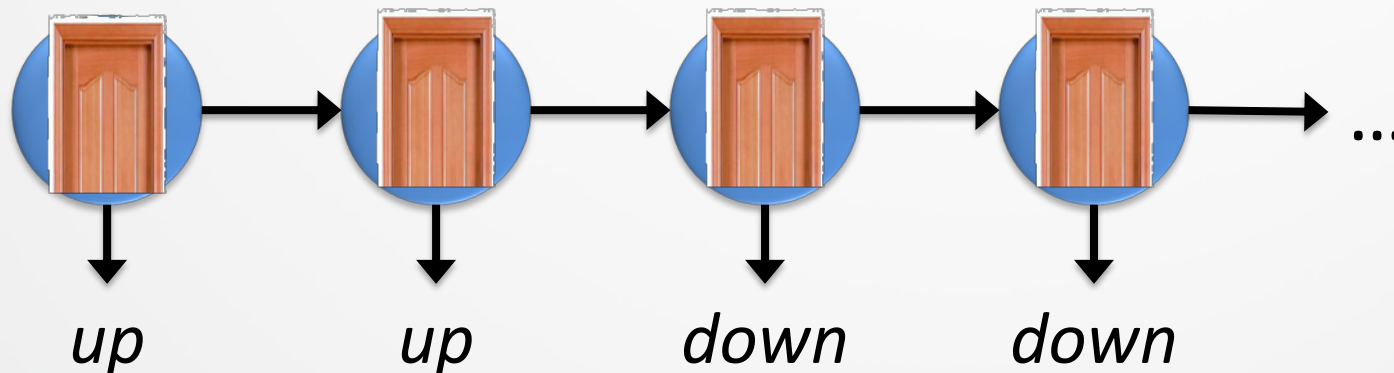


- A: Basically, the same as before.

- $P(q_i|q_{i-1}) = \frac{P(q_{i-1}q_i)}{P(q_{i-1})}$  is learned with MLE from training data.
- $P(w_i|q_i) = \frac{P(w_i, q_i)}{P(q_i)}$  is also learned with MLE from training data.

# Hidden variables

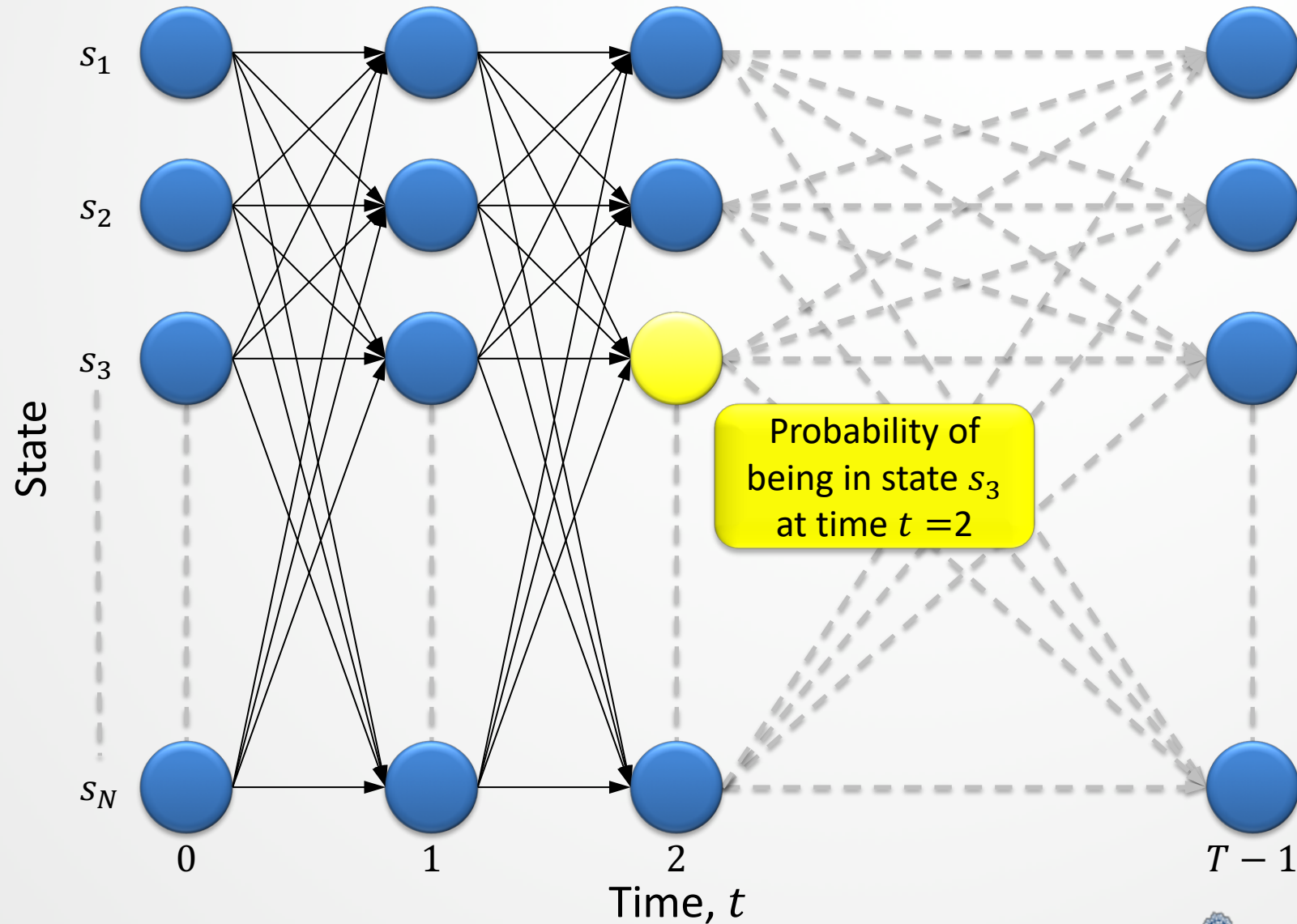
- Q: What if you **don't** have access to the **state** during testing?
  - e.g., you're asked to compute  $P(\langle up, up \rangle)$
- Q: What if you **don't** have access to the **state** during *training*?



# Tasks for HMMs

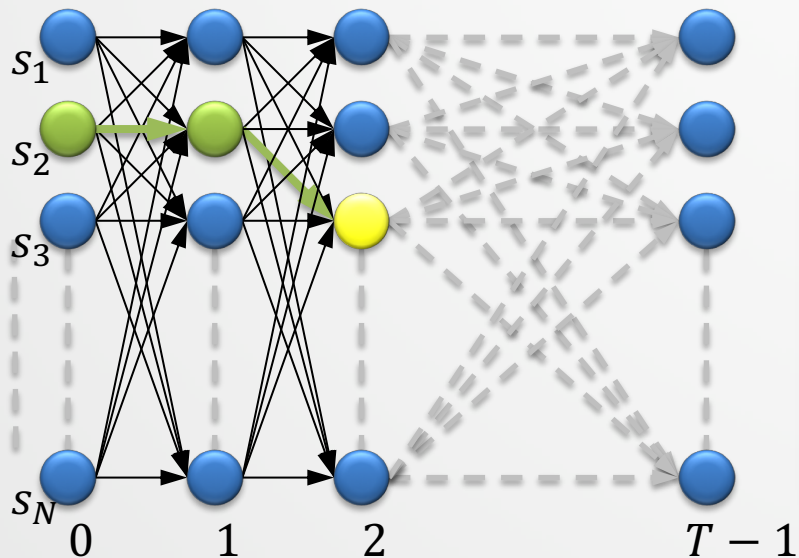
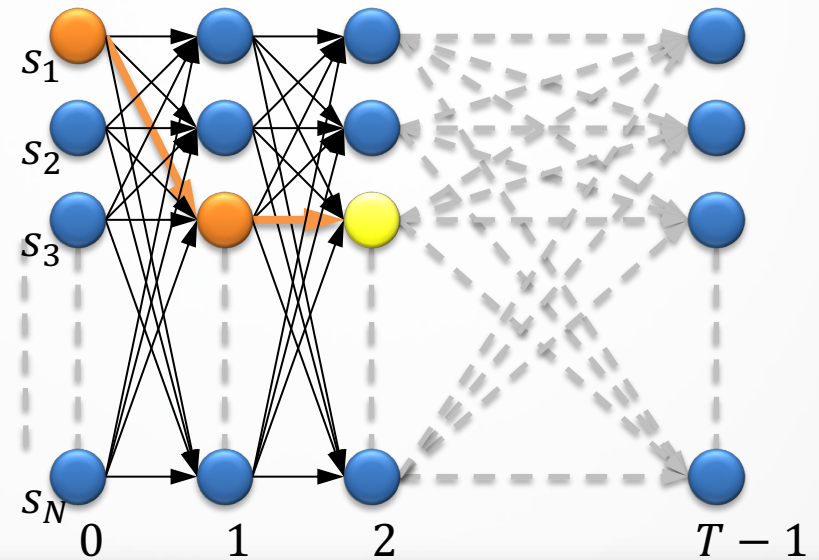
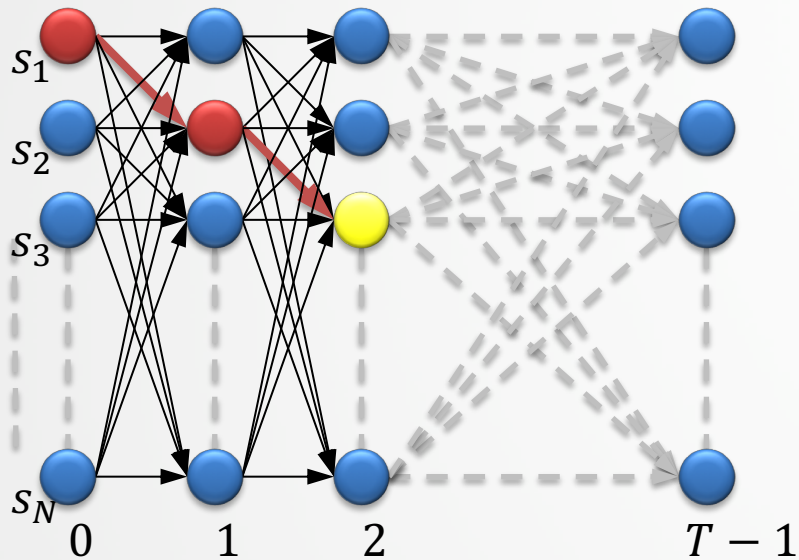
1. Given a **model** with particular parameters  $\theta = \langle \Pi, A, B \rangle$ , how do we efficiently **compute the likelihood** of a *particular observation sequence*,  $P(\mathcal{O}; \theta)$ ?
2. Given an **observation sequence**  $\mathcal{O}$  and a **model**  $\theta$ , how do we **choose a state sequence**  $Q = \{q_0, \dots, q_T\}$  that best explains the observations?
3. Given a large **observation sequence**  $\mathcal{O}$ , how do we **choose the best parameters**  $\theta = \langle \Pi, A, B \rangle$  that explain the data  $\mathcal{O}$ ?

# 1. Trellis





## 2. Choosing the best state sequence



I want to guess which sequence of states generated an observation.

E.g., if states are PoS and observations are **words**

## 2. The Viterbi algorithm

- Also an inductive dynamic-programming algorithm that uses the trellis.
- Define the probability of the most probable path leading to the trellis node at (state  $i$ , time  $t$ ) as

$$\delta_i(t) = \max_{q_0 \dots q_{t-1}} P(q_0 \dots q_{t-1}, \sigma_0 \dots \sigma_{t-1}, q_t = s_i; \theta)$$

- And the incoming arc that led to this most probable path is defined as  $\psi_i(t)$

# 3. Training HMMs

- We want to **modify** the parameters of our model  $\theta = \langle \Pi, A, B \rangle$  so that  $P(\mathcal{O}; \theta)$  is maximized for some **training** data  $\mathcal{O}$ :

$$\hat{\theta} = \operatorname{argmax}_{\theta} P(\mathcal{O}; \theta)$$

- If we want to choose a **best state sequence**  $Q^*$  on previously unseen **test data**, the parameters of the HMM should first be tuned to similar **training data**.

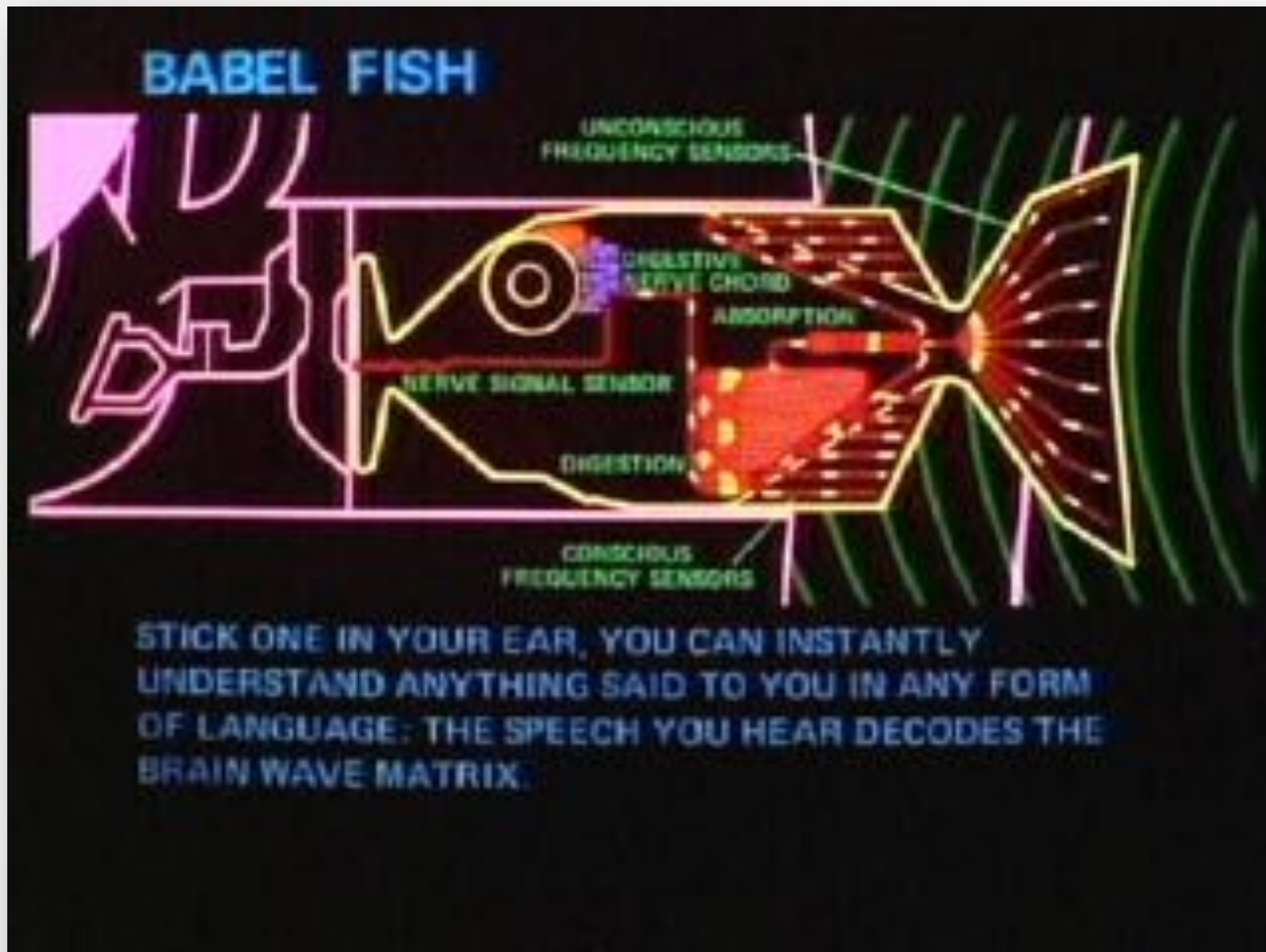
# 3. Expectation-maximization

- If we knew  $\theta$ , we could estimate **expectations** such as
  - Expected number of times in state  $s_i$ ,
  - Expected number of transitions  $s_i \rightarrow s_j$

- If we knew:
  - Expected number of times in state  $s_i$ ,
  - Expected number of transitions  $s_i \rightarrow s_j$then we could compute the **maximum likelihood estimate** of

$$\theta = \langle \pi_i, \{a_{ij}\}, \{b_i(w)\} \rangle$$

# Statistical machine translation



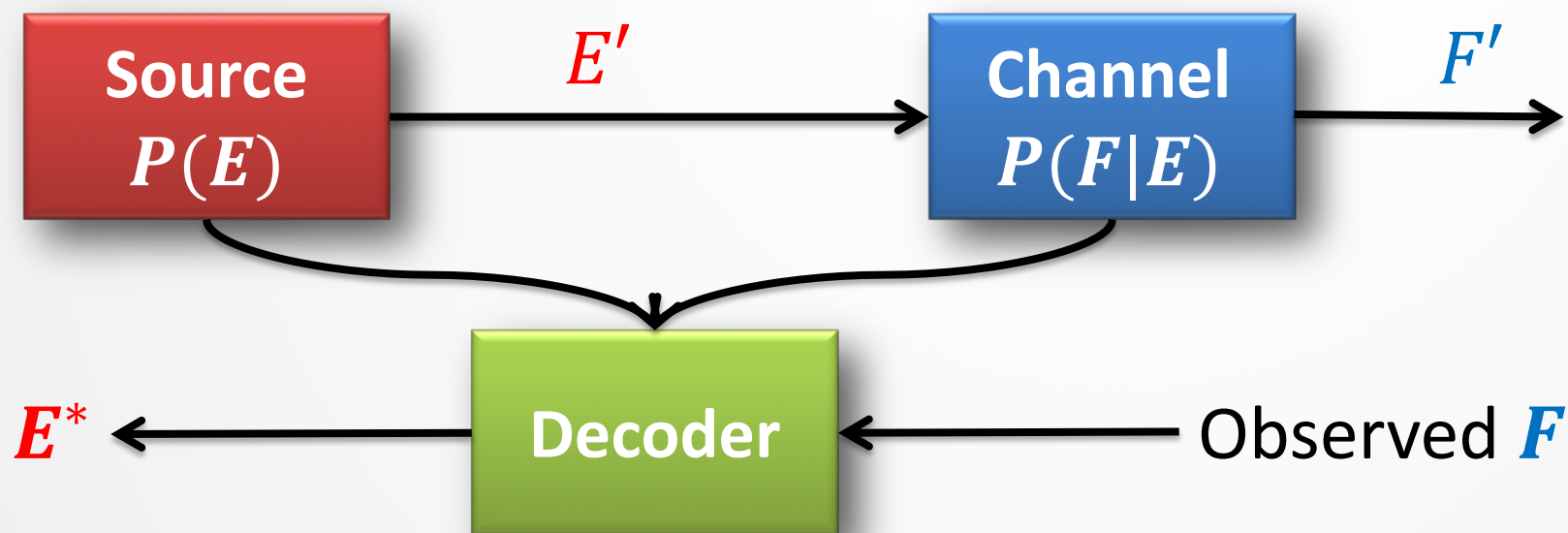
# Challenges of SMT

- Lexical ambiguity (e.g., words are polysemous).
  - Differing word orders.
  - Syntactic ambiguity.
  - Miscellaneous idiosyncracies.
- Sentence alignment.
    - **Gale&Church**: alignment by length (minimize costs).
    - **Church**: *cognates* approximated by 4-graphs.
    - **Melamed**: *cognates* approximated by longest common subsequences.

# The noisy channel

Language model

Translation model

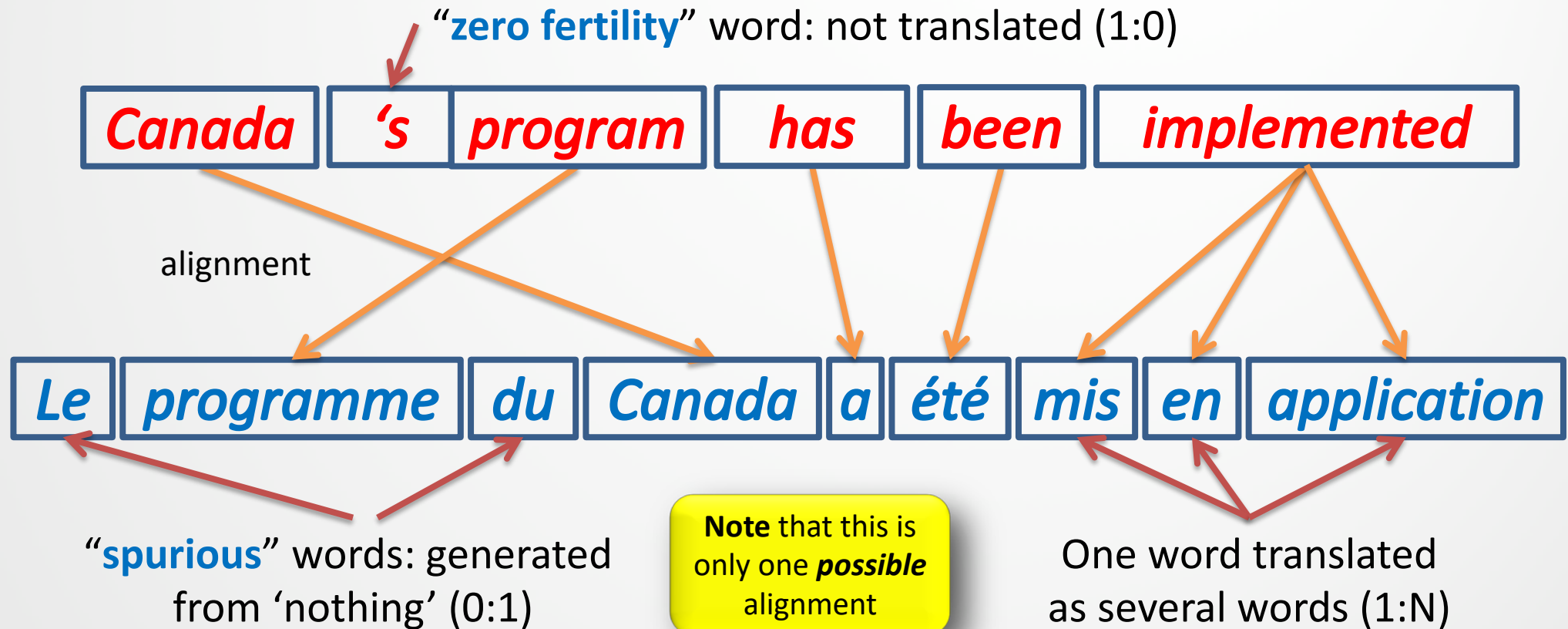


$$E^* = \operatorname{argmax}_E P(F|E)P(E)$$

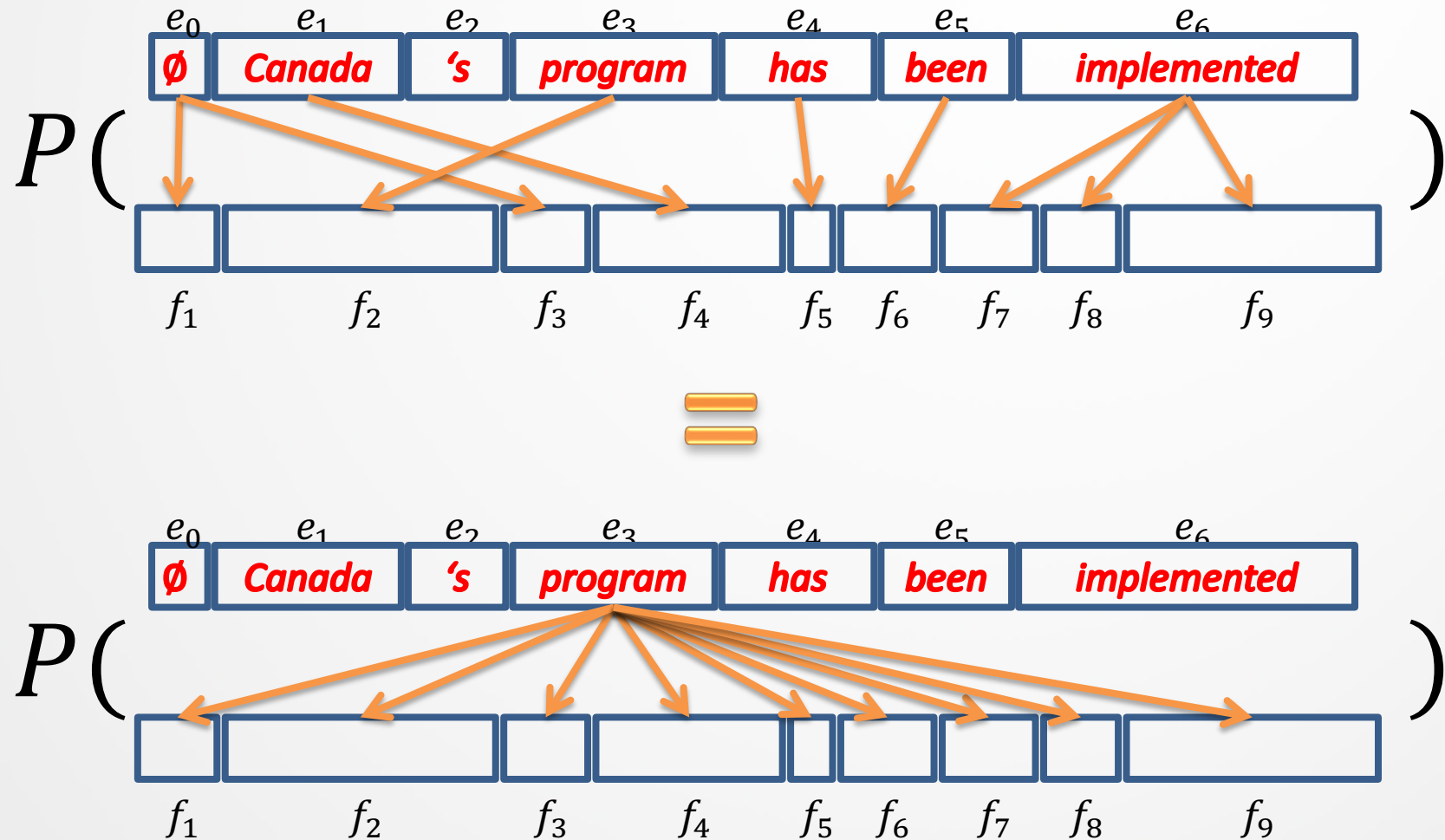


# Word alignment


- Word alignments can be 1:1, N:1, 1:N, 0:1, 1:0,... E.g.,



# IBM Model 1 assumption



# IBM Model 1: EM

1. **Initialize** translation parameters randomly (or uniformly).
2. **Expectation:** Compute expected value of  $Count(e, f)$  for all words in training data  $\mathcal{O}$ , given your current translation parameters,  $\theta_k$ .  

3. **Maximization:** Compute the maximum likelihood estimate of the parameters based on the expected counts, giving improved parameters,  $\theta_{k+1}$ .

# IBM Model 1: EM



$$P(F|a, E) = P(\text{maison}|\text{blue}) \times \\ P(\text{bleue}|\text{house}) = \frac{1}{3} \cdot \frac{1}{3} = \frac{1}{9}$$



$$P(F|a, E) = P(\text{la}|\text{the}) \times \\ P(\text{maison}|\text{house}) = \frac{1}{3} \cdot \frac{1}{3} = \frac{1}{9}$$

1. Take the **product** of each  $p(e)$  with each alignments and sentence pair.
2. **Normalize** by summing over all alignments for each sentence.
3. **Add** the appropriate normalized counts for each French/English word pair to find tcount (and total).
4. Use tcount and total to **re-estimate**  $p(f|e)$ .

(See lecture 6)

$$P(\text{la}|\text{house}) = \frac{1}{3} \cdot \frac{1}{3} = \frac{1}{9}$$

# Bilingual evaluation: BLEU

- In lecture 6-2,  $\|\text{Ref1}\| = 16$ ,  $\|\text{Ref2}\| = 17$ ,  $\|\text{Ref3}\| = 16$ , and  $\|\text{Cn1}\| = 18$  and  $\|\text{Cn2}\| = 14$ ,

$$\text{brevity}_1 = \frac{17}{18} \quad BP_1 = 1$$

$$\text{brevity}_2 = \frac{16}{14} \quad BP_2 = e^{1 - \left(\frac{8}{7}\right)} = 0.8669$$

- Final score** of candidate  $C$ :

$$BLEU = BP \times (p_1 p_2 \dots p_n)^{1/n}$$

where

$$p_n = \frac{\sum_{ngram \in C} \text{Count}_R(ngram)}{\sum_{ngram \in C} \text{Count}_C(ngram)}$$

Reference

Candidate

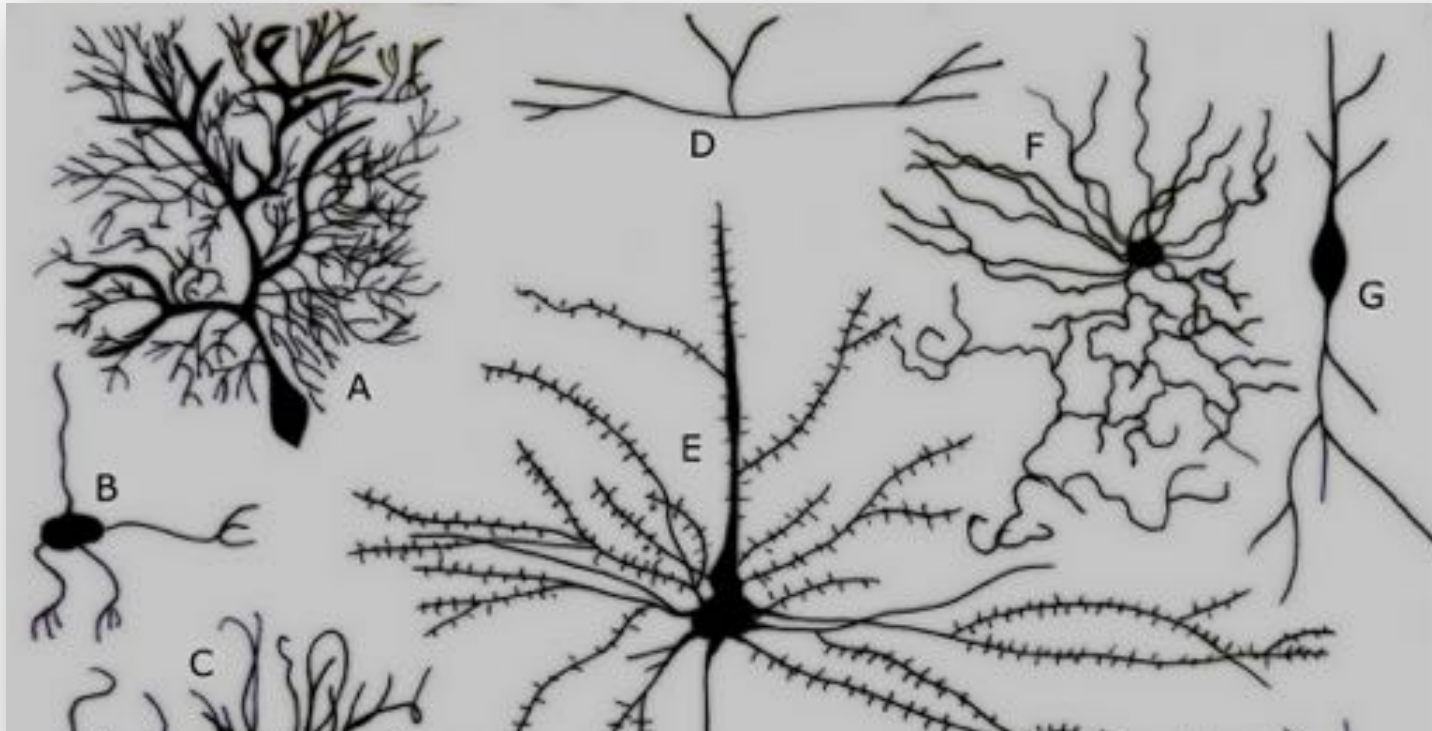
# BLEU example

- **Reference 1:** *I am afraid Dave*
- **Reference 2:** *I am scared Dave*
- **Reference 3:** *I have fear David*
- **Candidate:** *I fear David*

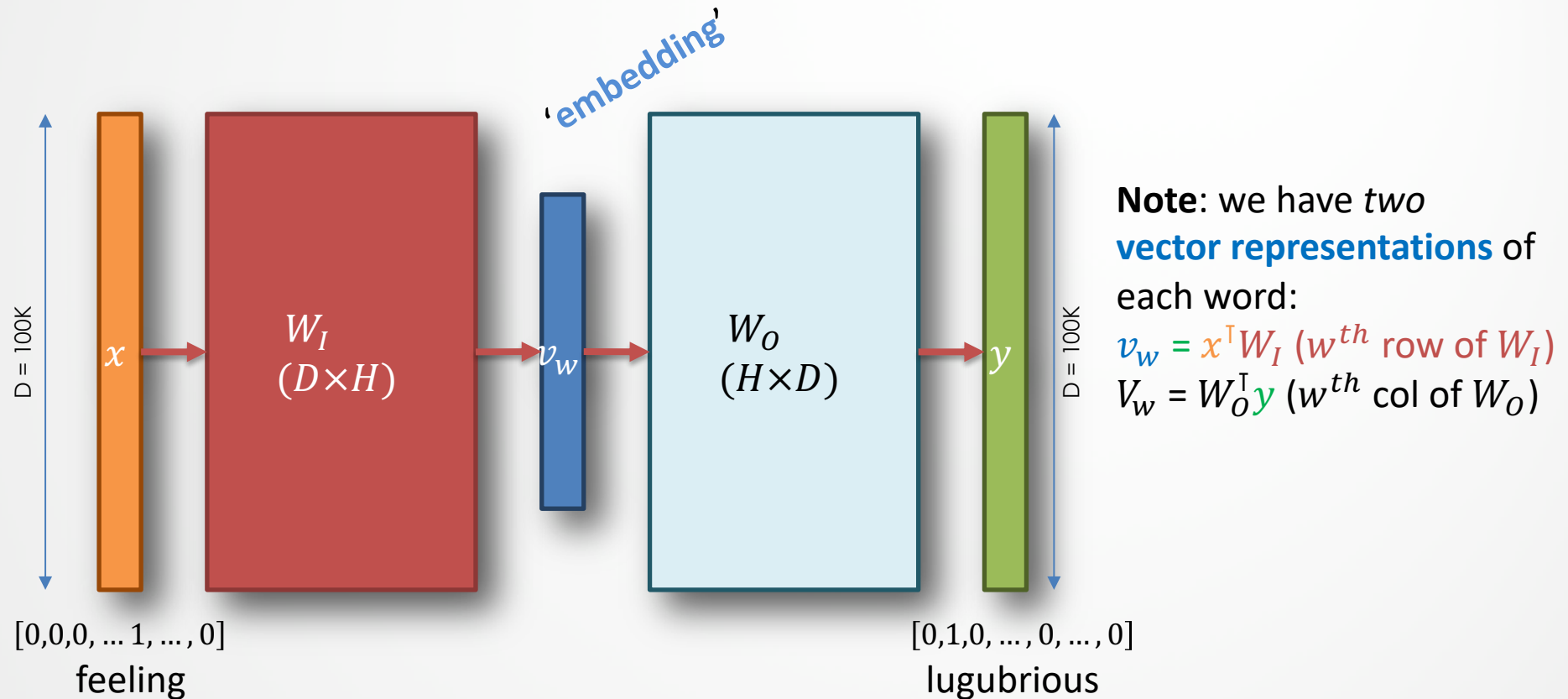
Assume  $cap(n) = 2$  for all  $n$ -grams

- $brevity = \frac{4}{3} \geq 1$  so  $BP = e^{1 - \left(\frac{4}{3}\right)}$
- $p_1 = \frac{\sum_{1gram \in C} Count_R(1gram)}{\sum_{1gram \in C} Count_C(1gram)} = \frac{1+1+1}{1+1+1} = 1$
- $p_2 = \frac{\sum_{2gram \in C} Count_R(2gram)}{\sum_{2gram \in C} Count_C(2gram)} = \frac{1}{2}$
- $BLEU = BP(p_1 p_2)^{\frac{1}{2}} = e^{1 - \left(\frac{4}{3}\right)} \left(\frac{1}{2}\right)^{\frac{1}{2}} \approx 0.5067$

# Neural language models



# Continuous bag of words (1 word context)



feeling    lugubrious    all  
a    lugubrious    sadness  
...

**'softmax':**  $P(w_o | w_i) = \frac{\exp(V_{w_o}^T v_{w_i})}{\sum_{w=1}^W \exp(V_w^T v_{w_i})}$

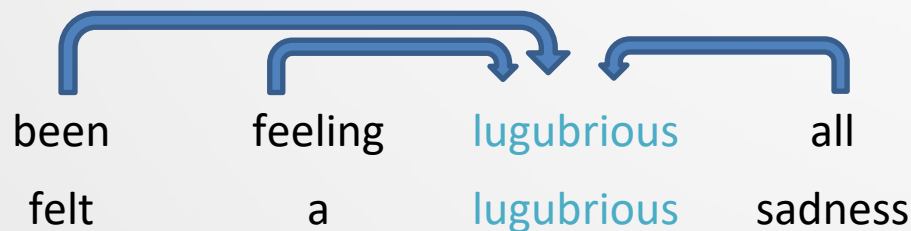
Where

$v_w$  is the 'input' vector for word  $w$ ,  
 $V_w$  is the 'output' vector for word  $w$ ,

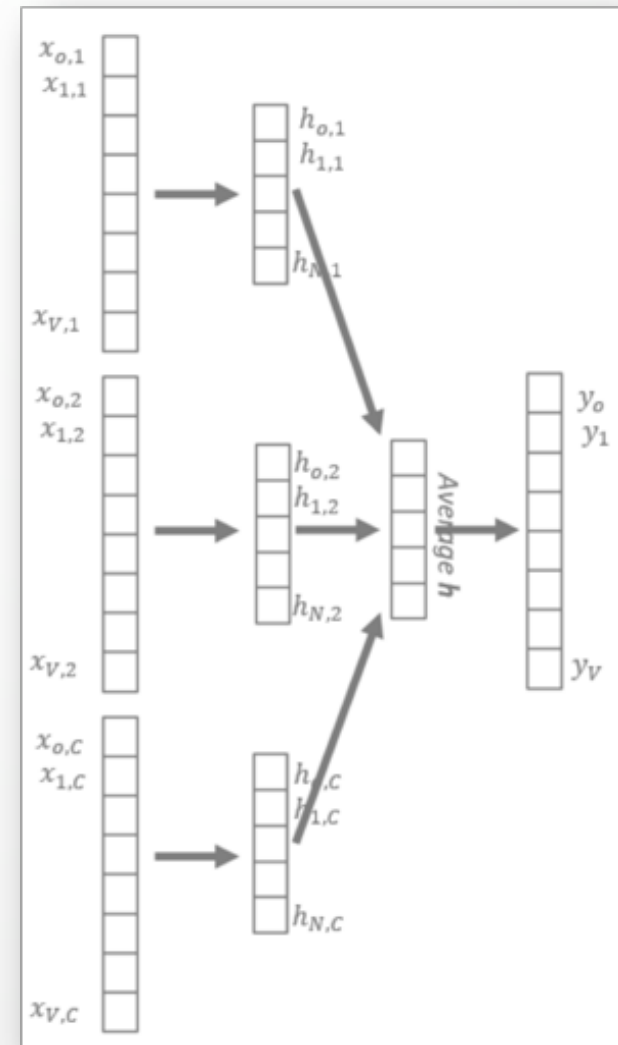


# Continuous bag of words ( $C$ words context)

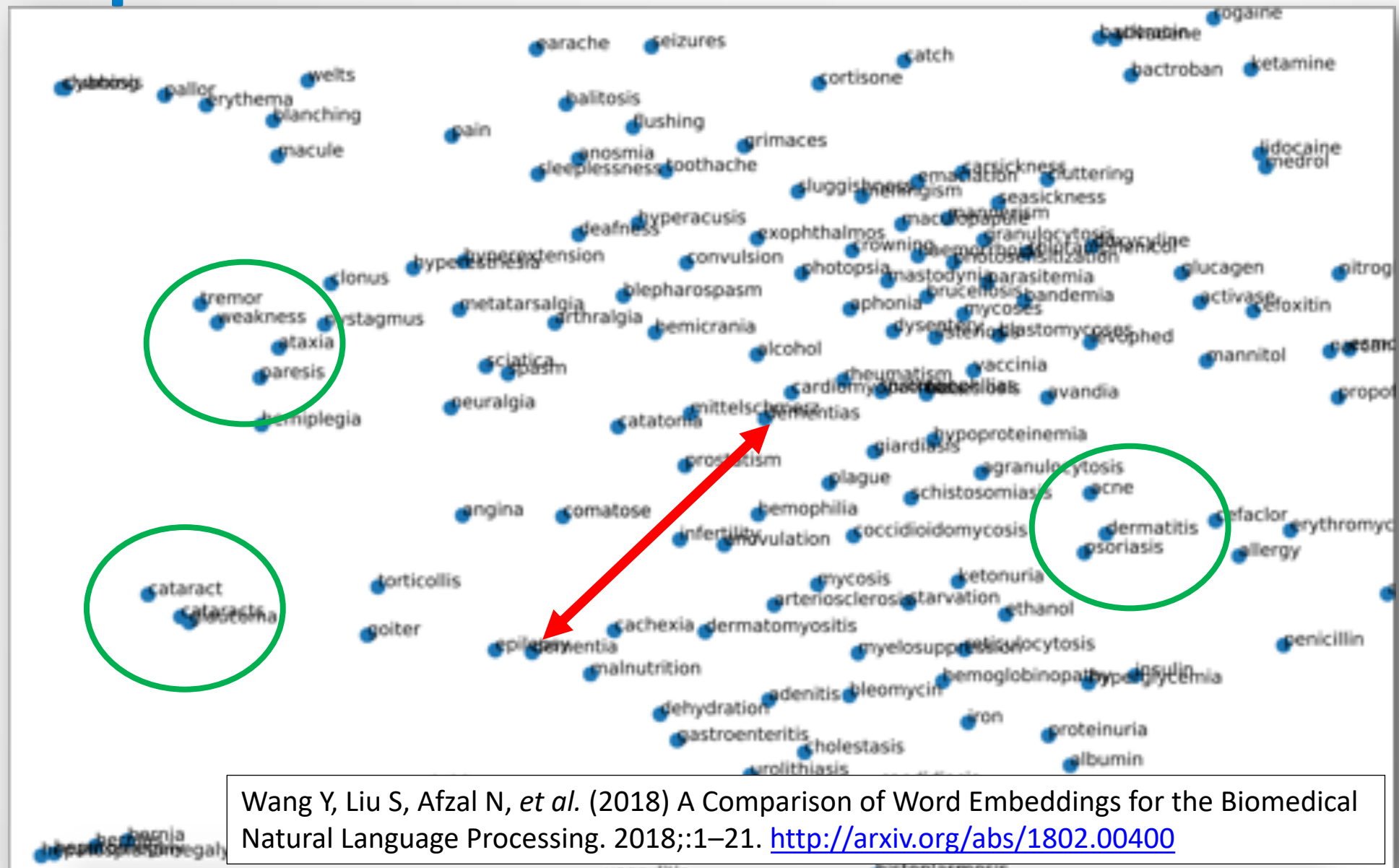
- If we want to use **more context**,  $C$ , we need to change the network architecture somewhat.
  - Each input word will produce one of  $C$  embeddings
  - We just need to add an **intermediate layer**, usually this just averages the embeddings.



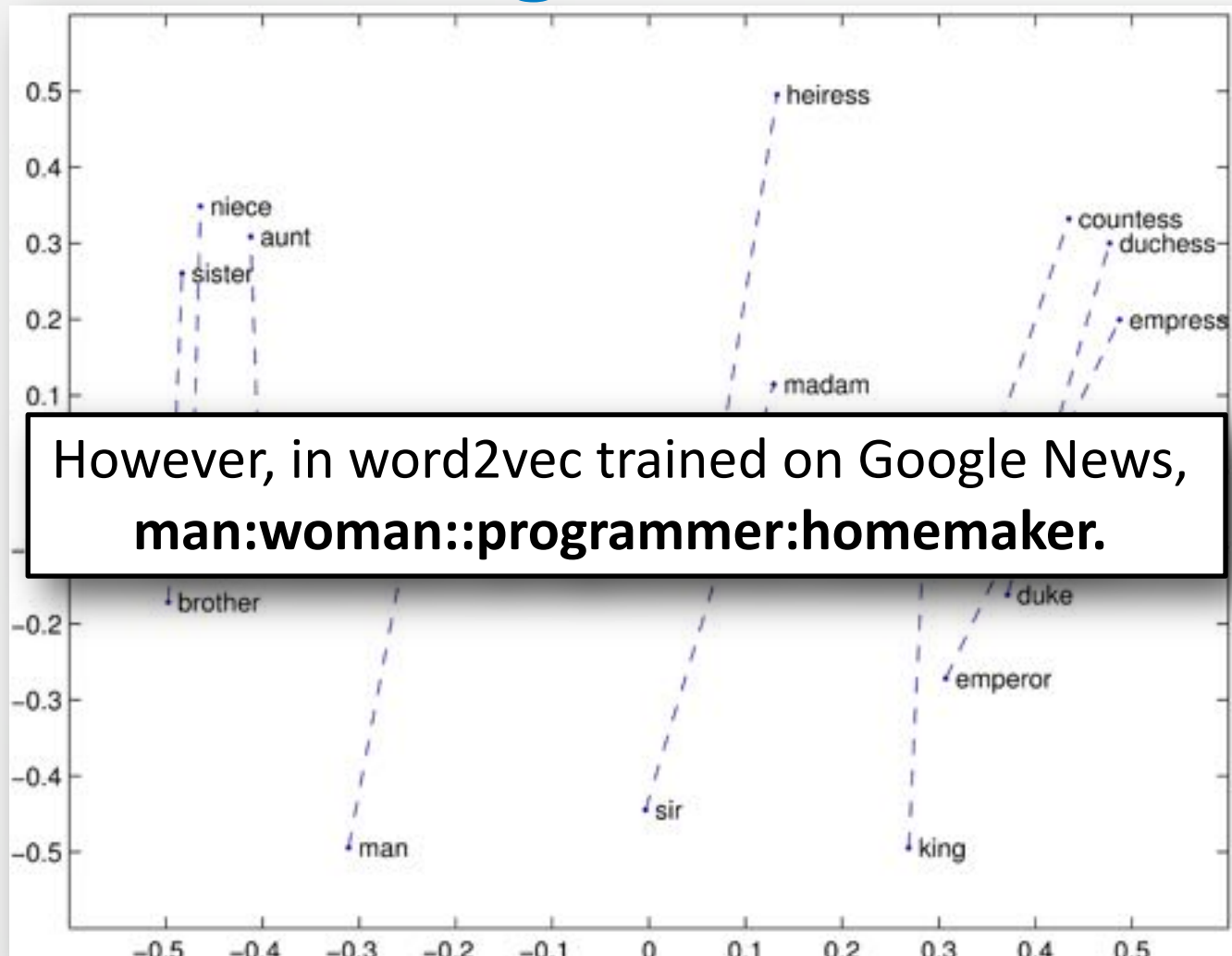
...



# Importance of in-domain data



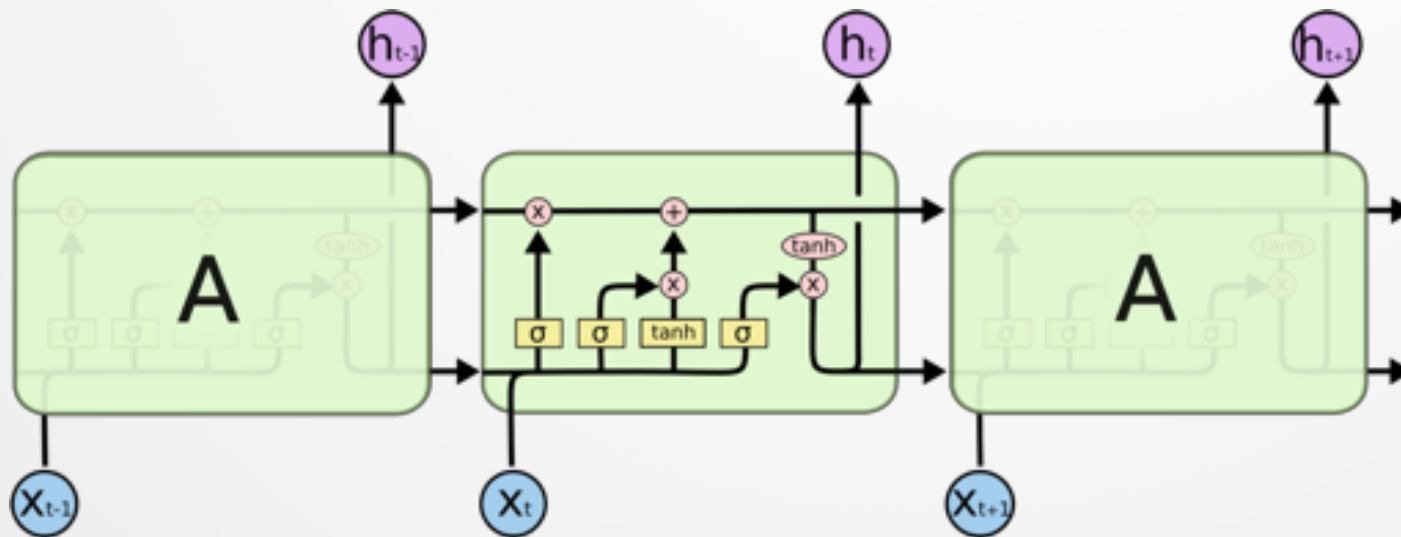
# Let's talk about gender at the UofT



Bolukbasi T, Chang K, Zou J, *et al.* Man is to Computer Programmer as Woman is to Homemaker? Debiasing Word Embeddings. In: *NIPS*. 2016. 1–9.

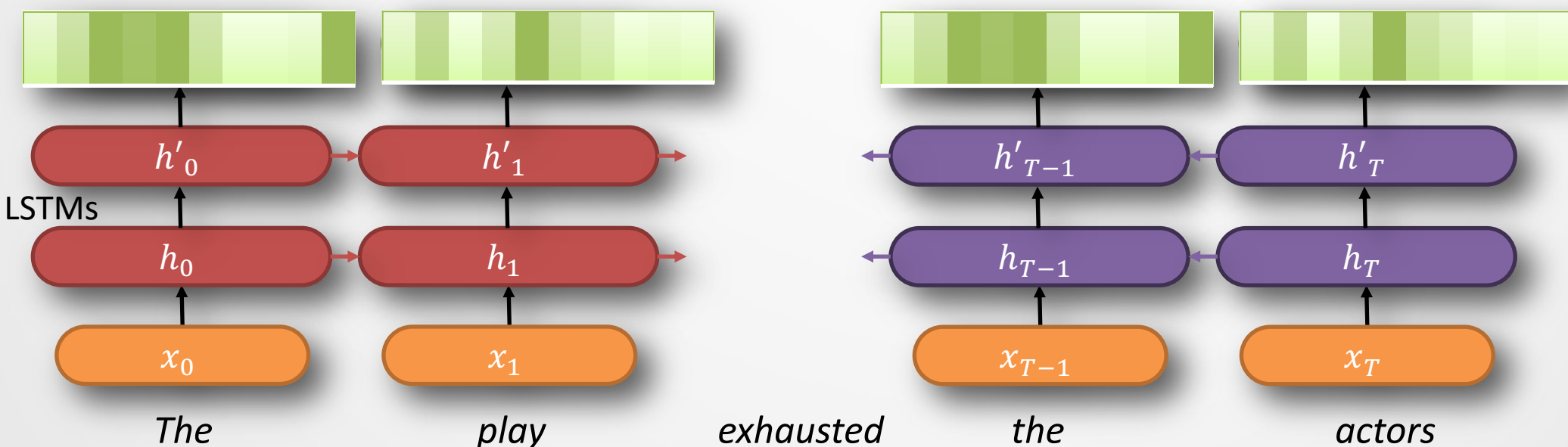
# Recurrent neural networks

- Consider RNNs generally, and LSTMs and others, specifically
- **Hint:** How do these models differ and how they are similar?  
What are their **strengths** and **weaknesses**?
- What are the components of an LSTM network?



# ELMo: Embeddings from Language Models

- Instead of a fixed embedding for each word **type**, ELMo considers the entire sentence before embedding each **token**.
  - It uses a bi-directional LSTM trained on a specific task.
  - Outputs are softmax probabilities on words, as before.



# Automatic speech recognition

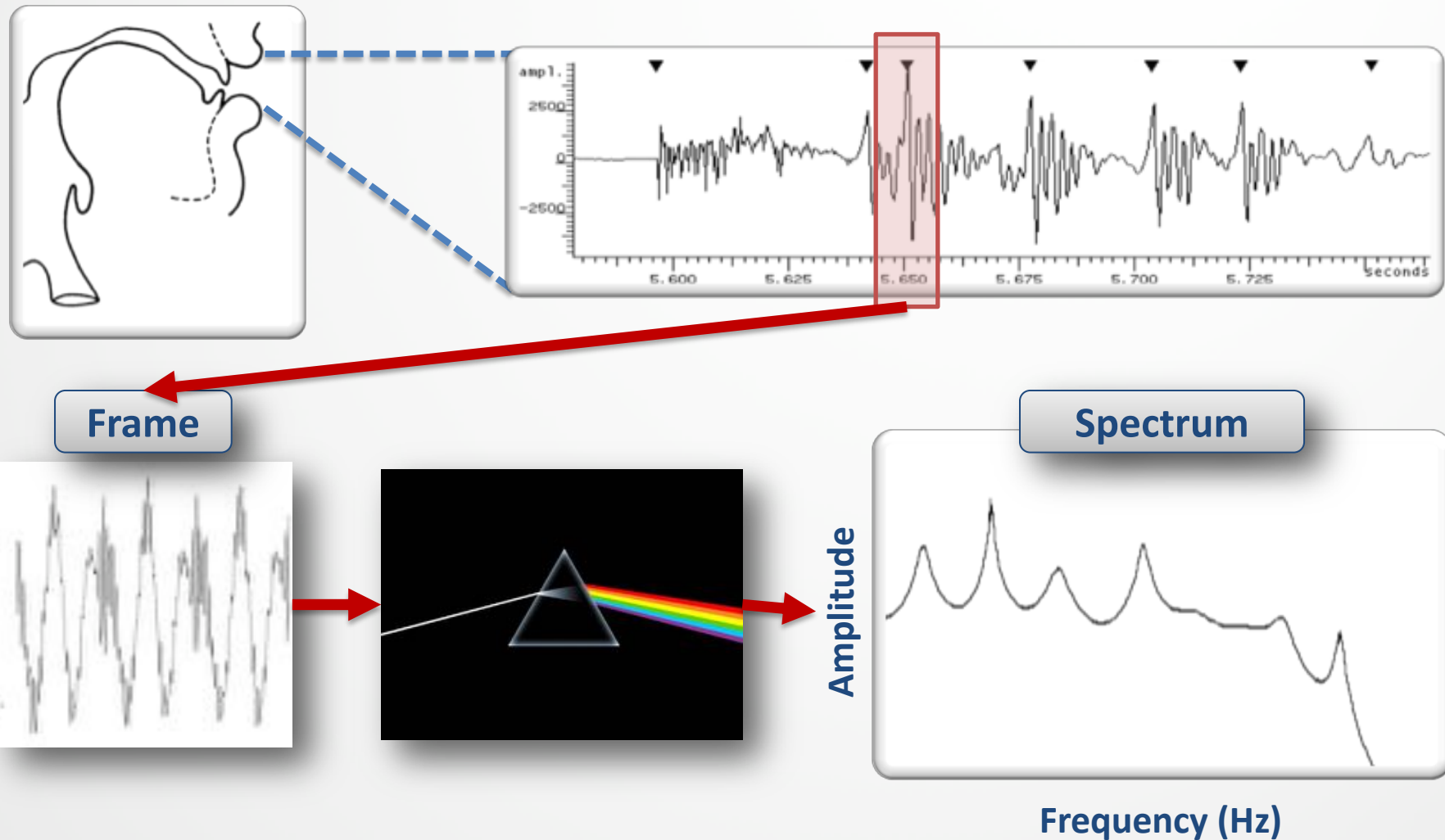


# Manners of articulation

- **Phoneme:** *n.* a distinctive unit of speech sound.
- English phonemes can be partitioned into groups, e.g.,:
  - **Stops/plosives:** complete vocal tract constriction and burst of energy (e.g., 'papa').
  - **Fricatives:** noisy, with air passing through a tight constriction (e.g., 'shift').
  - **Nasals:** involve air passing through the nasal cavity (e.g., 'mama').
  - **Vowels:** open vocal tract, no nasal air.
  - **Glides/liquids:** similar to vowels, but typically with more constriction (e.g., 'wall').



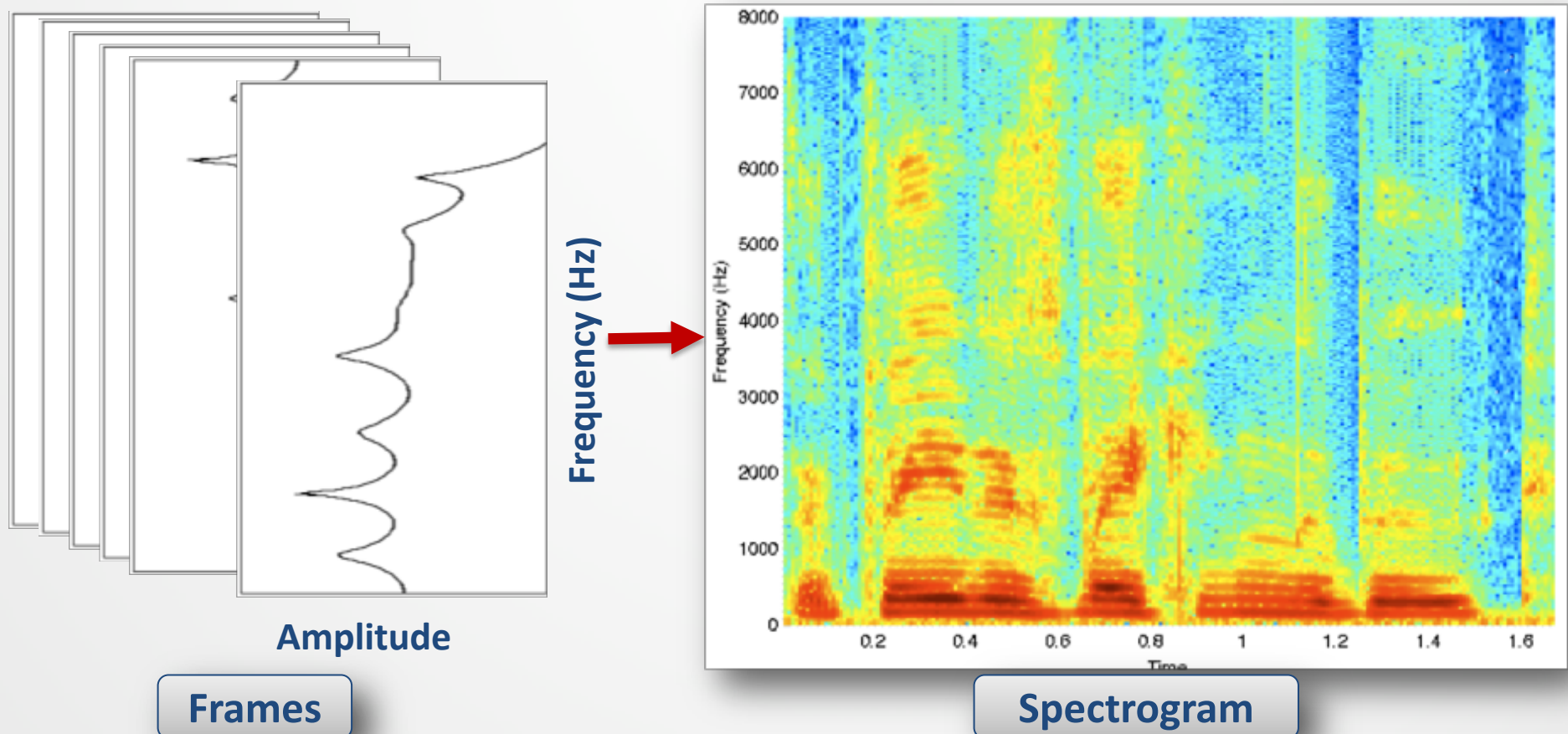
# Windowing and spectra





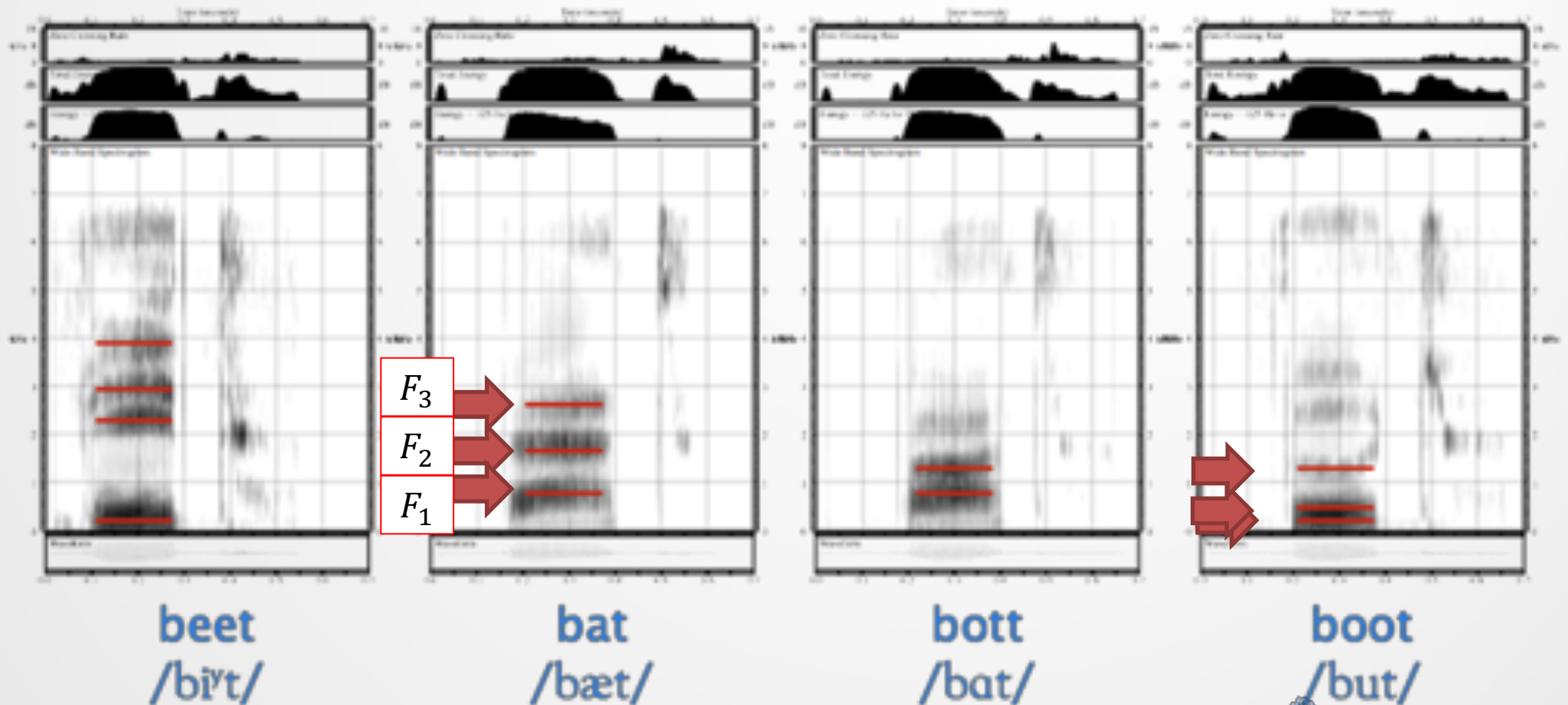
# Spectrograms

- **Spectrogram:** *n.* a 3D plot of amplitude and frequency over time.

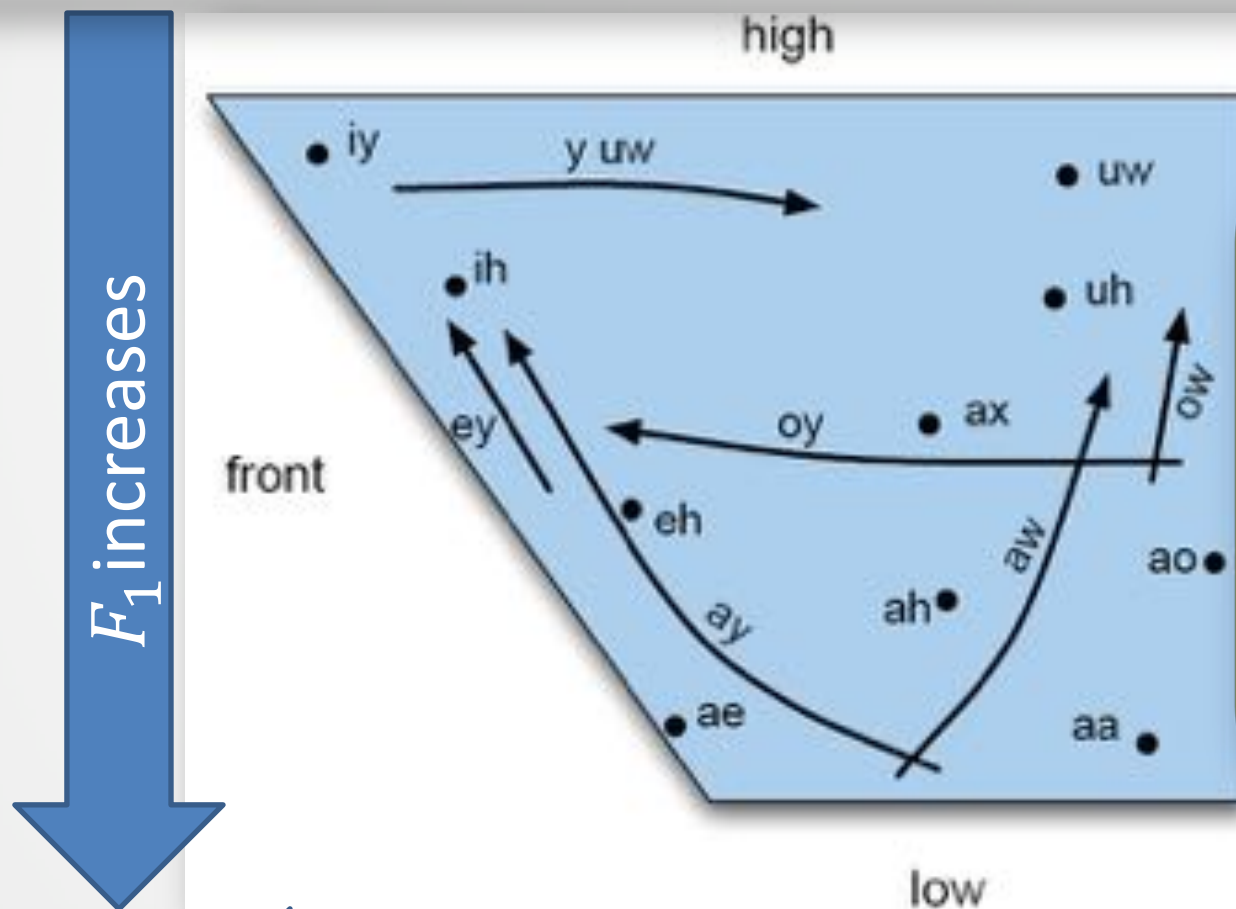


# Formants and phonemes

- **Formant:** *n.* A large concentration of energy within a band of frequency (e.g.,  $F_1$ ,  $F_2$ ,  $F_3$ ).



# The vowel trapezoid



If I asked you about phonemes, I'd probably give you example words.

e.g., *iy* as in *sheet*

# Prosody

- **Sonorant**: *n.* Any **sustained** phoneme in which the **glottis** is vibrating (i.e., the phoneme is '**voiced**').
  - Includes some consonants (e.g., /w/, /m/, /g/).
- **Prosody**: *n.* the **modification** of speech acoustics in order to convey some **extra-lexical** meaning:
  - **Pitch**: Changing of  $F_0$  over time.
  - **Duration**: The length in time of sonorants.
  - **Loudness**: The amount of **energy** produced by the **lungs**.

# Mel-frequency cepstral coefficients

- **Mel-frequency cepstral coefficients (MFCCs)** are the most popular representation of speech used in ASR.
  - They are the spectra of the logarithms of the mel-scaled filtered spectra of the windows of the waveform.



- Based on what we know about human perception of sound and the source-filter model.

# Classifying speakers

- The speech produced by **one speaker** will cluster *differently* in MFCC space than speech from **another speaker**.
  - We can  $\therefore$  decide if a given observation comes from one speaker or another.

|      |     | Time, $t$ |     |     |     |
|------|-----|-----------|-----|-----|-----|
|      |     | 0         | 1   | ... | T   |
| MFCC | 1   |           |     | ... |     |
|      | 2   |           |     | ... |     |
|      | 3   |           |     | ... |     |
|      | ... | ...       | ... | ... | ... |
|      | 42  |           |     | ... |     |

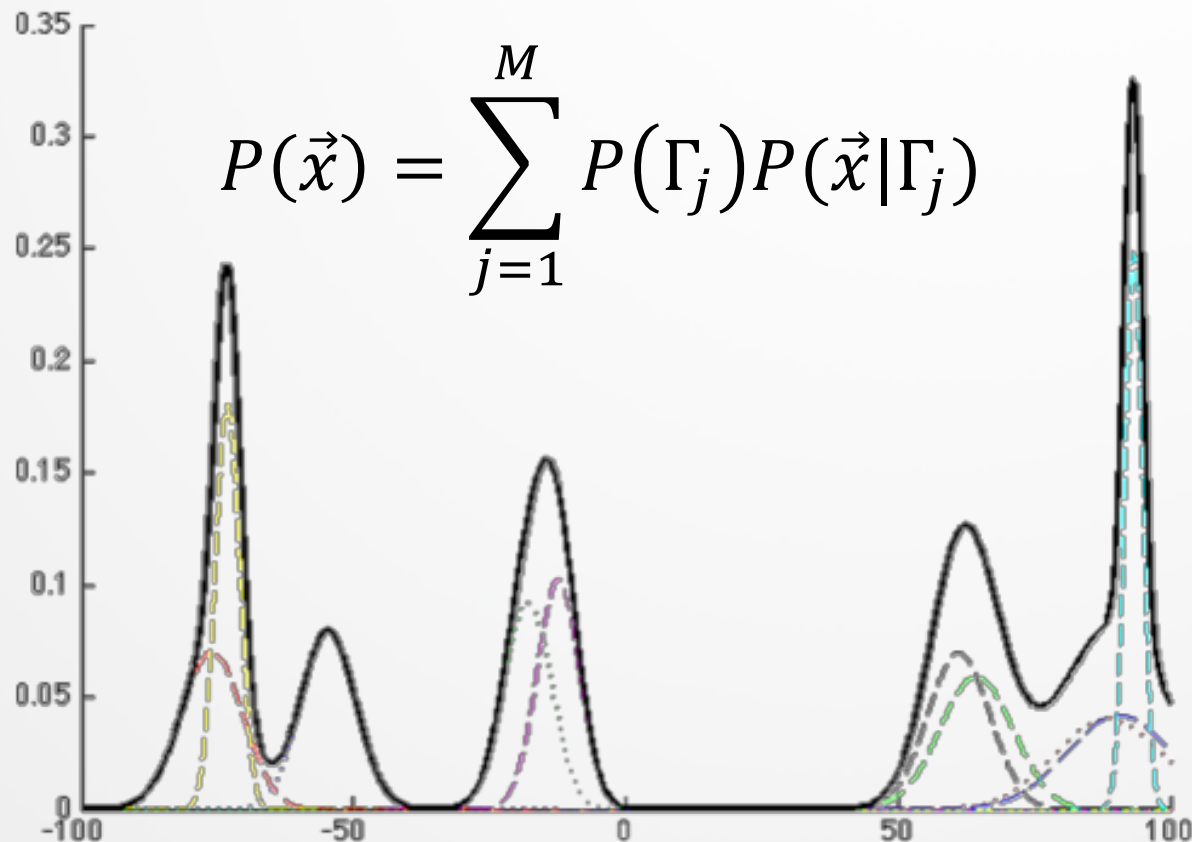
Observation matrix

$$P(\text{orange bar} \mid \text{woman on phone}) > P(\text{orange bar} \mid \text{man in uniform})$$

# Mixtures of Gaussians

- **Gaussian mixture models (GMMs)** are a weighted linear combination of  $M$  component Gaussians,  $\langle \Gamma_1, \Gamma_2, \dots, \Gamma_M \rangle$  such that

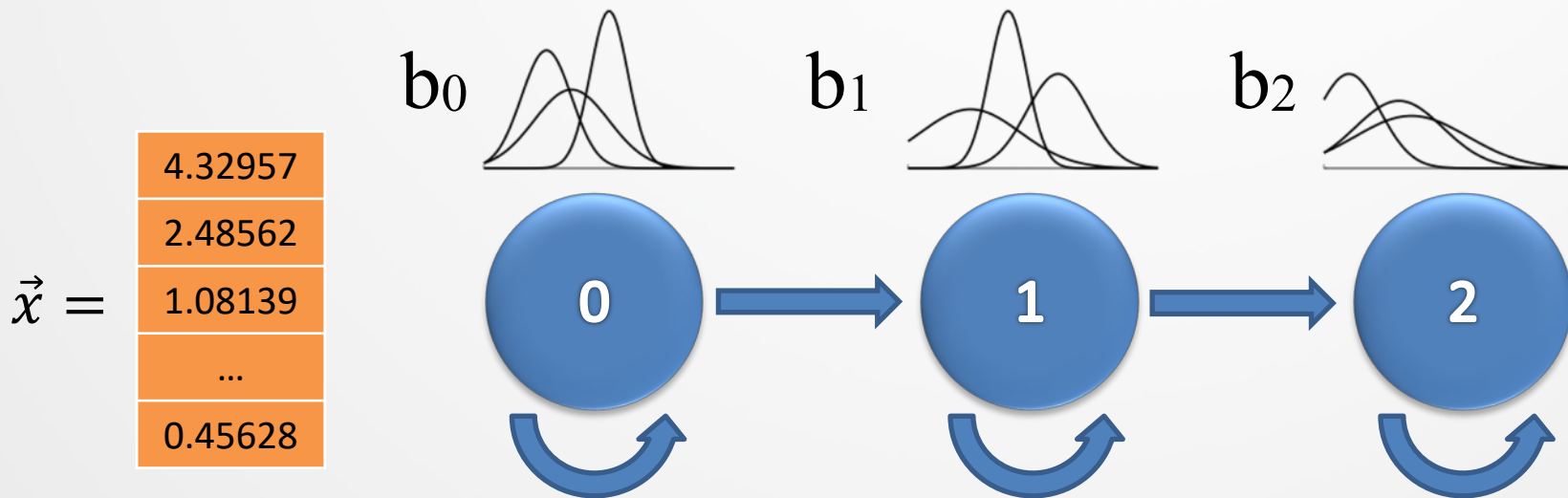
$$P(\vec{x}) = \sum_{j=1}^M P(\Gamma_j)P(\vec{x}|\Gamma_j)$$





# Continuous HMMs

- Previously we saw **discrete HMMs**: at each state we observed a discrete symbol from a finite set of discrete symbols.
- A **continuous HMM** has observations that are distributed over continuous variables.
  - Observation probabilities,  $b_i$ , are also continuous.





# Levenshtein distance

|           |           |   | hypothesis |    |       |   |      |       |  |
|-----------|-----------|---|------------|----|-------|---|------|-------|--|
|           |           | - | how        | to | wreck | a | nice | beach |  |
| Reference | -         | 0 | ∞          | ∞  | ∞     | ∞ | ∞    | ∞     |  |
|           | how       | ∞ | 0          | 1  | 2     | 3 | 4    | 5     |  |
|           | to        | ∞ | 1          | 0  | 1     | 2 | 3    | 4     |  |
|           | recognize | ∞ | 2          | 1  | 1     | 2 | 3    | 4     |  |
|           | speech    | ∞ | 3          | 2  | 2     | 2 | 3    | 4     |  |

- See the example in lecture 8-2. **Work it out yourself.**

# Speech synthesis



# Speech synthesis

- **Text-to-speech**: *n.* the conversion of electronic text into equivalent, audible speech waveforms.
- Three **architectures** for performing speech synthesis:
  - Formant synthesis,
  - Concatenative synthesis,
  - Articulatory synthesis.
- How do they differ? What are their (dis)advantages?
- Common **components** of speech synthesis:
  - **Letter-to-sound rules** and dictionaries,
  - Acoustic prosody modification.

# Final thoughts

(not thoughts on the final)

# NLC in industry



# Final thoughts

- This course **barely** scratches the surface of these beautiful topics. Talk to these people:



Graeme  
Hirst



Gerald  
Penn



Frank  
Rudzicz



Suzanne  
Stevenson



Yang  
Xu

- Many of the techniques in this course are applicable **generally**.
- Now is a great time to make fundamental **progress** in this and adjacent areas of research.





# Aside – Knowledge

- **Anecdotes** are often useless except as proofs by contradiction.
  - E.g., “*I saw Google used as a verb*” does **not** mean that *Google* is **always** (or even **likely** to be) a verb, just that it is **not always** a noun.
- **Shallow statistics** are often not enough to be truly meaningful.
  - E.g., “*My ASR system is 95% accurate on my test data. Yours is only 94.5% accurate, you horrible knuckle-dragging idiot.*”
    - What if the test data was **biased** to favor my system?
    - What if we only used a **very small** amount of data?
- We need a **test** to see if our statistics actually **mean** something.

Find some way to be *comfortable*  
making *mistakes*



*Thank you*