

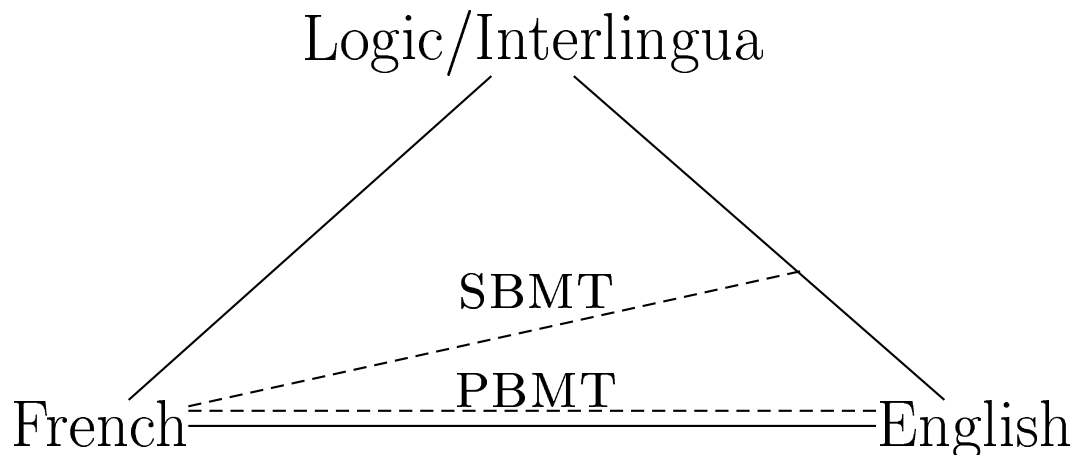
# Statistical Machine Translation

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## The Vauquois Triangle (1968)



A very influential geometric depiction of a quandry that haunted machine translation research for years: at what level of linguistic structure should the “transfer” be made?

Current statistical machine translation research is roughly divided into two camps: *phrase-based* and *syntax-based*. We’ll cover phrase-based MT.

## The IBM Translation Model

We want to find the best English translation of a given French sentence:

$$\hat{E} = \operatorname{argmax}_E p(E|F)$$

Apply Bayes's Rule:

$$\hat{E} = \operatorname{argmax}_E p(F|E) \cdot p(F)$$

...and for efficiency, make the assumption that there is a single very probable *alignment*,  $A$ , between the two strings:

$$\hat{E} \approx \operatorname{argmax}_E p(F, A|E) \cdot p(F)$$

(without this assumption, how would  $p(F|E)$  relate to  $p(F, A|E)$ ?)

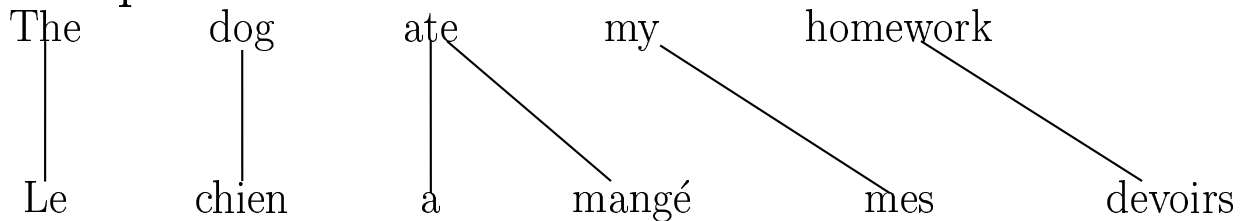
Just as in ASR,  $p(F)$  is a *language model*.  $p(F, A|E)$  is called a *translation model*.

## Alignments

An alignment is a mapping from the substrings of one string to the substrings of another. There are a lot of these.

So we restrict them, usually by limiting the sizes of the subsets that can correspond, often by limiting the *skew* of the correspondence between them.

Examples:



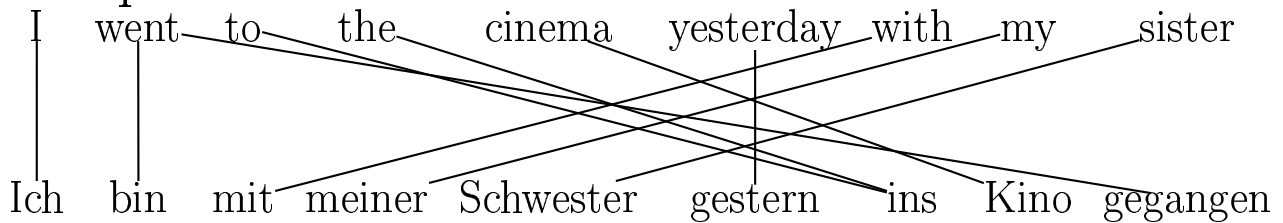
Here, for each French word, there is a unique English word that it is aligned with (size of substring on the French side is always 1), but not *vice versa*. Very little skew.

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Examples:



Same here for German, except lots of skew. The word order is almost completely reversed.

## Calculating Aligned Translation Model Probability

$$p(F, A|E) = \prod_{i=1}^{|E|} p(n(e_i)|e_i) \cdot \prod_{j=1}^{|F|} p(f_j|e_{a_j}) \cdot d(A|E, F)$$

where:

- $n(e_i)$  is the *fertility* of  $e_i$ . It indicates how many French words are aligned with  $e_i$ .
- $p(f_j|e_{a_j})$  is a *lexical transfer probability*. It indicates which words in English are likely to be aligned with which words in French.
- $d(A|F, E)$  is a *distortion probability*. It indicates the probability of a particular order of French words, given the words and their English counterparts.

We must optimize this function subject to the

constraint that  $\sum_{i=1}^{|E|} n(e_i) = |F|$ .

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Fertility and lexical transfer are estimated by training on bilingual corpora that are annotated with alignments (*bitexts*).

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Distortion is often handled by a combination of heuristics and statistical estimates of very language-pair-specific word order transformations, e.g., French  $N_1 \text{ de } N_2 \longrightarrow N_2 N_1$  in English.