

167 Express formally that specification  $R$  is satisfied by any number (including 0) of repetitions of behavior satisfying specification  $S$ .

After trying the question, scroll down to the solution.

§ Here are three answers:

$$R \Leftarrow ok \vee (S.R)$$

$$R \Leftarrow ok \vee (R.S)$$

$$R \Leftarrow ok \vee S \vee (R.R)$$

Taking the last answer:

$$\begin{aligned} & R \\ \Leftarrow & ok \vee S \vee (R.R) && \text{given} \\ \Leftarrow & ok \vee S \vee (ok \vee S \vee (R.R). ok \vee S \vee (R.R)) && \text{by monotonicity} \\ \Leftarrow & ok \vee S \vee (ok.ok) \vee (ok.S) \vee (ok.R.R) \vee (S.ok) \vee (S.S) \vee (S.R.R) && \text{distribution} \\ & \vee (R.R.ok) \vee (R.R.S) \vee (R.R.R.R) \\ = & ok \vee S \vee (S.S) \vee (R.R) \vee (S.R.R) \vee (R.R.S) \vee (R.R.R.R) \end{aligned}$$

So now we have 0, 1, and 2 repetitions and some other stuff. Further applications of monotonicity and distribution give us more repetitions.