

331 Let  $a$  and  $b$  be binary expressions with unprimed variables, and let  $A, B, C, P, Q, R, S, T$ , and  $U$  be implementable specifications such that the refinements

$A \Leftarrow \text{if } a \text{ then } ok \text{ else if } b \text{ then } P. B \text{ else } Q. C \text{ fi fi}$

$B \Leftarrow \text{if } a \text{ then } ok \text{ else if } b \text{ then } R. C \text{ else } S. A \text{ fi fi}$

$C \Leftarrow \text{if } a \text{ then } ok \text{ else if } b \text{ then } T. A \text{ else } U. B \text{ fi fi}$

are all theorems. Then  $A$  can be executed as follows (using  $\text{\%}$  for labeling):

$A\text{\%} \text{ if } a \text{ then go to } D \text{ else if } b \text{ then } P. \text{ go to } B \text{ else } Q. \text{ go to } C \text{ fi fi.}$

$B\text{\%} \text{ if } a \text{ then go to } D \text{ else if } b \text{ then } R. \text{ go to } C \text{ else } S. \text{ go to } A \text{ fi fi.}$

$C\text{\%} \text{ if } a \text{ then go to } D \text{ else if } b \text{ then } T. \text{ go to } A \text{ else } U. \text{ go to } B \text{ fi fi.}$

$D\text{\%} ok$

We have replaced refinement and call with labeling and **go tos**.

- (a) Show that it is not possible to replace refinement and call (in this example) with **while** loops without introducing any new variables.
- (b) Show that it is possible to replace refinement and call (in this example) with **while** loops if you introduce new variables.

no solution given