

480 Let  $a$  and  $b$  be integer variables. Refine  $a' = a+b \wedge b' = a-b$  by replacing the question marks in the following. Prove that your answer is a refinement.

(a)  $a := ? . b := ?$

(b)  $b := ? . a := ?$

(c)  $a := ? \parallel b := ?$

After trying the question, scroll down to the solution.

(a)	$a := ?. \ b := ?$	
§	$a := a+b. \ b := a - 2 \times b$	expand second assignment
=	$a := a+b. \ a' = a \wedge b' = a - 2 \times b$	substitution law
=	$a' = a+b \wedge b' = a-b$	
(b)	$b := ?. \ a := ?$	
§	$b := a-b. \ a := 2 \times a - b$	expand second assignment
=	$b := a-b. \ a' = 2 \times a - b \wedge b' = b$	substitution law
=	$a' = a+b \wedge b' = a-b$	
(c)	$a := ? \parallel b := ?$	
§	$a := a+b \parallel b := a-b$	partition
=	$a' = a+b \wedge b' = a-b$	