

## ***csc444h: software engineering I***

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## ***announcements***

- one a2 left to be handed back
- lab tomorrow for demo/questions
- presentations next week, scrum standup meetings in lab next week

## **APPLIED RESEARCH IN ACTION 2015**

**TUESDAY, DECEMBER 1  
4:00 - 7:00 PM**

Join us for a showcase of R&D internship projects by the 2014 cohort of the Master of Science in Applied Computing (MScAC) program.

DEPARTMENT OF COMPUTER SCIENCE  
INNOVATION LAB (DCSIL)  
GERSTEIN SCIENCE INFORMATION CENTRE  
9 KING'S COLLEGE CIRCLE, 2ND FLOOR  
TORONTO, ON

RSVP [uoft.me/aria2015](http://uoft.me/aria2015)

## ***effort estimation***

## estimates

- estimates are never 100% certain
- ex. we may estimate a feature to be 20 ECDs (ideal 8-hour developer days)
  - are we saying it will be done in 20 ECDs? no.
  - so, then what exactly are we saying?
    - is it optimistic?
    - pessimistic?
    - how confident are we in it?
- a quantity whose value depends upon unknowns (or randomness) is called a *stochastic variable* - our plan is full of these!

## estimation techniques

Source: Adapted from van Vliet, 1999, section 7.3.5

- function points  
 $FP = a_1I + a_2O + a_3E + a_4L + a_5F$   
the  $a_i$ s are “weighting factors”
  - $I$  = number of user inputs (data entry)
  - $O$  = number of user outputs (reports, screens, error msgs)
  - $E$  = number of user queries
  - $L$  = number of files
  - $F$  = number of external interface (other devices, systems)
- an example might be:  
 $FP = 4I + 5O + 4E + 10L + 7F$

## estimation techniques (2)

- three-point estimating
  - tends to provide better estimate than asking for a range
    - $w$  = worst-case estimate
    - $m$  = most likely estimate
    - $b$  = best-case estimate

$$E = \sum_i \frac{w_i + 4m_i + b_i}{6}$$

## confidence intervals

- toss a coin 5000 times
  - expect heads about half the time (2500)
  - exactly 2500? only about 1.1%
  - $\leq 2500$ ? chance is 50%, on repeated experiments, half will be  $\leq 2500$ , half will be  $> 2500$
  - $\leq 2530$ ? chance is now about 80%
  - $\leq 2550$ ? chance is now about 92%
- these (50%, 80%, 92%) are called confidence intervals
  - with 80% confidence we can say that the number of heads will be less than 2530

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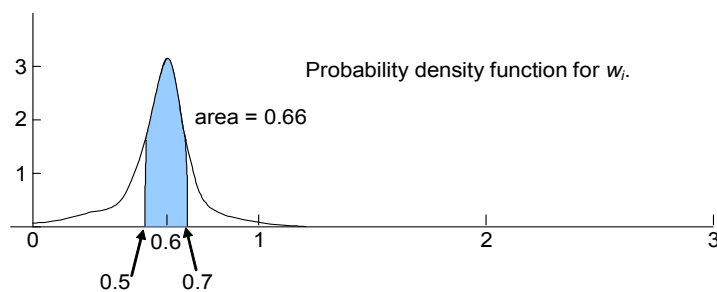
how do you estimate when a feature will be done with 80% confidence?

## stochastic variables

- consider a developer with a work factor,  $w$ 
  - $w$  (even measured) is a stochastic variable
  - stochastic variables are described by statistical distributions
  - a statistical distribution will tell you:
    - for any range of  $w$ , the probability of  $w$  being within that range
  - can be described completely with a probability density function (PDF)
    - x-axis: possible range of the variable
    - y-axis: numbers (density)  $\geq 0$
    - probability the value is between two values,  $a$  and  $b$ , is the area under the PDF between  $a$  and  $b$

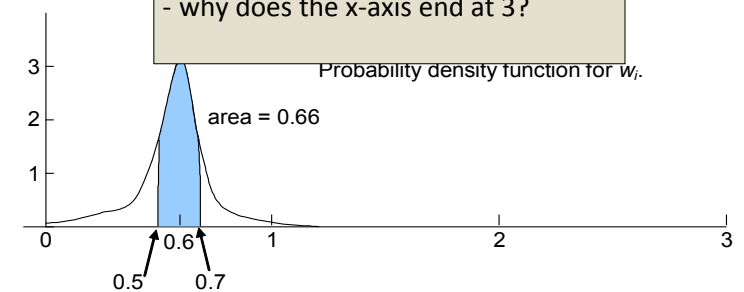
## PDF for work factor

- probability that  $0.5 < w < 0.7 = 66\%$
- looks to be fairly accurate in practice
  - finite probability of being 0
  - not much chance of being bigger than 1.2 or so



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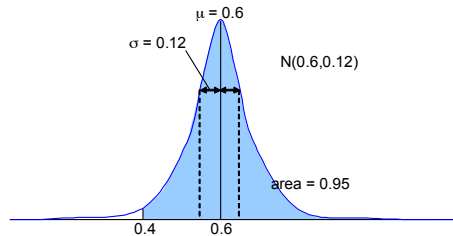
use  $w = 0.6$  if you don't have any previous data

why is there a chance of  $w = 0$ ?

why does the x-axis end at 3?

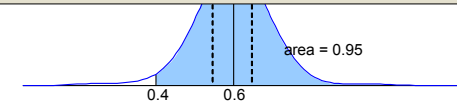
## normal for work factor

- assume work factor is described by a normal distribution
- 2-points needed to fit a normal, average case, and some reasonable “worst case”
  - avg. case, half the time less, half more = 0.6
  - “worst” case: 95% of the time  $w$  won’t be that bad = 0.4
    - normal that fits is  $N(0.6, 0.12)$



## normal for work factor

- assume work factor is described by a normal distribution
  - normal distribution is easy to work with because it’s symmetric about the mean
- using normal is ok because (human) estimation errors are likely to dominate over the choice of PDF
- normal extends to  $\infty$  in both directions, so we are working with a cutoff version...but not cutting much



## back to estimation

- ex. for a feature estimate of 1 week
  - post-facto
    - what are the units?
    - 40 hrs? longer? shorter? dedicated? disrupted (calendar)? one developer? two?
  - stochastic
    - 1 week best case?
    - 1 week worst case?
    - 1 week average case?
    - need a PDF
- depending on these concerns, my “1 week” may be someone else’s 4 weeks!

## stochastic capacity constraint

- $T$  is fixed
- $F$  and  $N$  are both stochastic variables
- can only speak about the chance of all the features fitting in the release or sprint
- say  $F = 400$ ,  $N = 10$ , and  $T = 40$ , are we good to go?
  - can’t say for sure
  - need precise distributions for  $F$  and  $N$  to answer, and then, only with some confidence interval

## summing distributions

- $F$  and  $N$  are sums over many contributing stochastic variables.
  - ex.  $F = f_1 + f_2$
  - if  $f_1$  and  $f_2$  have associated statistical distributions, what is the distribution of  $F$ ?
    - in general case, no answer
  - however, if  $f_1$  and  $f_2$  are both normal, then
    - $F$  is also normal
    - mean of  $F$  is sum of means of  $f_1$  and  $f_2$
    - standard deviation of  $F$  is the square root of the sum of squares of the standard deviations of  $f_1$  and  $f_2$

## law of large numbers

- if we sum lots and lots of stochastic variables, the sum will approach a normal distribution
- therefore, something like  $F$  is going to be pretty close to normal (for large releases, or longer horizons)
  - ex. dozens of feature estimates summed up
- $N$  will also be close to normal, but probably less so
  - ex. 5 developer's work factors summed up

## delta statistic

- $D(T) = N \times T - F$  (delta)
- we have normal approximations for  $N$  and  $F$  and can compute the normal curve for  $D$  as a function of various values for  $T$
- we are interested in  $P(D(T) \geq 0)$ 
  - the probability all features will be finished on time
  - negative delta means it's late!
- in choosing  $T$  (assuming we can) we want a confidence interval the company can live with
- ex. if the company can live with an 80% confidence interval, choose  $T$  such that  $D(T) \geq 0$  80% of the time

## example: picking $T$

		confidence level						
		25%	40%	50%	60%	80%	90%	95%
	30	-39	-77	-100	-123	-177	-217	-250
	35	14	-26	-50	-74	-130	-172	-207
	40	67	25	0	-25	-84	-128	-164
<b>T</b>	45	121	77	50	23	-38	-85	-123
	50	174	128	100	72	7	-41	-82
	55	228	179	150	121	52	1	-41
	60	282	231	200	169	97	44	0

- $F$  is normal with mean 400 and 90% worst case 500
- $N$  is normal with mean 10 and 90% worst case 8
- cells are  $D(T) = N \times T - F$  at the indicated confidence level
- important is transition through 0

## example: picking $T$ (2)

		confidence level						
		25%	40%	50%	60%	80%	90%	95%
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	55	228	179	150	121	52	1	-41
	60	282	231	200	169	97	44	0

- 95% chance of hitting dates, choose  $T = 60$ , or...
- $T = 40 \Rightarrow$  only a 5% chance of being > 20 days late
- to be 80% sure, select  $T = 49$
- gamble with only a 25% chance, pick  $T = 33$

## shortcut

- ask for 80% worst case estimates for features
- if  $F = N \times T$  using the 80% worst case values, then there is an 80% chance of finishing on time
- deterministic release plan can be based on this approach
- note: if you also ask for average cases you can fit a normal curve for  $D(T)$  and predict  $P(D(T)) < 0$  (i.e. missing the date)

*the end*