

Types

Since each expression has a type, each definition also has a type.

- `square n = n*n`
then `square` has type `Integer -> Integer`
(Ok, it really is something more generic, but let me lie for once more.)
- `myNumber = square 10`
then `myNumber` has type `Integer`

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Specifying Types

- You can specify the type of an expression or a subexpression:
`10 + 12 :: Integer` --specifies the whole expression
`10 + (12 :: Integer)` --specifies the 12
- You can also specify the type of a definition. Write it on a separate line.
`square :: Integer -> Integer`
`square n = n * n`
- Generally, `x::T` is pronounced as “x has type T”.

You may omit such specifications. Then Haskell will compute the most “generic” types possible.

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Defining Your Own Types

Let us define a colour type. It will be like an enumerated type.

- ```
data Colour = Red | Green | Blue
```
- The name of the new type is `Colour`.
  - Its possible values are: `Red`, `Green`, `Blue`.

Note:

- `Red`, `Green`, `Blue` are called *constructors* of `Colour`: they produce values of the type.
- Type names and constructor names must begin with capital letters.

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## Writing Functions for Your Types

Let us define a function that maps `Colour` to integer RGB codes.

```
Red goes to 255×2^{16} , Green goes to 255×2^8 , Blue goes to 255.
toRGB :: Colour -> Int
toRGB c = case c of
 Red -> 255 * 216
 Green -> 255 * 28
 Blue -> 255
```

This is just like procedural languages. Is there a more elegant way?

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## Writing Functions for Your Types (cont.)

More elegant way:

```
toRGB :: Colour -> Int
toRGB Red = 255 * 216
toRGB Green = 255 * 28
toRGB Blue = 255
```

Execution view:

- Computer compares the actual parameter with the formal parameters.
- Computer selects the first equation that matches.

This is called *pattern matching*.

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## How to Write a Function

Human conceptual view:

- I want Red to be mapped to  $255 \times 2^{16}$ .
- toRGB Red =  $255 * 2^{16}$
- I also want Green to be mapped to  $255 \times 2^8$ .
- toRGB Green =  $255 * 2^8$
- I also want Blue to be mapped to 255.
- toRGB Blue = 255

This is how you should write a function or read one.

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## More Examples of Functions

More functions written with pattern matching. Try to get used to them.

- Straightforward factorial.

```
factorial :: Integer -> Integer
factorial 1 = 1
factorial n = n * factorial (n-1)
```

- Smart factorial.

```
smartfact :: Integer -> Integer
smartfact n = f 1 n
 where f p 1 = p
 f p i = f (p*i) (i-1)
```

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## A More Interesting Type

Let us define a shape type. A shape will be a rectangle or an ellipse.

- A rectangle will have a width and a height.
  - An ellipse will have a width and a height too (lengths of the axes).
- Kind of like a union type.

```
data Shape = Rectangle Float Float
 | Ellipse Float Float
```

Now each constructor takes some parameters.

E.g., `Rectangle` takes two floating-point numbers, a width and a height. (Unfortunately the syntax only lets us write the types.)

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## A More Interesting Type (cont.)

Some expressions of type Shape:

```
Rectangle 1.0 2.0 :: Shape
Ellipse 2.0 3.0 :: Shape
```

If you enter them at a Haskell prompt, you'll get an error message:

```
ERROR: Cannot find "show" function for:
*** Expression : Rectangle 1.0 2.0
*** Of type : Shape
```

The computer is saying, "I don't know how to display data of this type."

How do we fix the stupid computer?

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## A More Interesting Type (cont.)

Add a line "deriving Show" at the end of the type declaration:

```
data Shape = Rectangle Float Float
 | Ellipse Float Float
 deriving Show
```

This tells the computer, "just display data of this type naively."

Now you can enter:

```
Rectangle 1.0 2.0
```

And the computer will display it.

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## A More Interesting Function

Let us write a function to compute areas of shapes.

```
area :: Shape -> Float
```

- Area of rectangle is width times height.

```
area (Rectangle w h) = w * h
```

The parentheses are needed when there are parameters to the constructor.

- Area of ellipse is  $\pi$  times width times height.  

```
area (Ellipse w h) = pi * w * h
```
- Done!

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## Constructor vs Function

Consider again:

```
Rectangle 1.0 2.0 :: Shape
```

- The constructor is acting like a function:

```
Rectangle :: Float -> Float -> Shape
```

In fact you can use it as such.

- So Red, Green, Blue are like functions requiring no parameters.
- But constructors and functions are different. E.g., cannot use functions in pattern matching.

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## An Introduction to Lists

Some example lists:

```
[False, True, False] :: [Bool]
[Rectangle 1.0 2.0, Ellipse 2.0 3.0] :: [Shape]
[] --the empty list, pronounced nil
```

- We will discuss the type of `[]` later. For now, it just works.
- Because of strong typing, Haskell lists are *homogeneous*: all elements in a list must be of the same type.

To simulate heterogeneous lists, use `list of a union type`, just like how we mix rectangles and ellipses in the same list.

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## An Introduction to Lists (cont.)

- The operator `:` adds an element to the front of a list.  
`False:[True]` gives `[False, True]`
- In fact, `[]` and `:` are constructors of the list types.  
`[] :: [Bool]`  
`(:) :: Bool -> [Bool] -> [Bool]`

So you can use them in pattern matching.

- `[False, True]` is really constructed in these stages:
  1. start with constructor `[]`
  2. use constructor `:` to add `True`. `True:[]`
  3. use constructor `:` to add `False`. `False:True:[]`

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## A Function Of List

Write a function that adds up a list of integers.

```
addList :: [Integer] -> Integer
```

- Hey I know how to do it when the list is empty.  
`addList [] = 0`
- If the list is not empty, then it is like `x:xs`, where `x` is the first number and `xs` is the rest of the list. I will add `x` to the sum of `xs`.  
The sum of `xs` is, of course, `addList xs`.  
`addList (x:xs) = x + addList xs`

- Done!

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## A More Interesting Function of List

Write a function that adds up the areas in a list of shapes.

```
arealist :: [Shape] -> Float
```

- Again, I know how to deal with the empty list.  
`arealist [] = 0`
- If the list is like `x:xs`, I will compute the area of `x`, then add it to the sum of the areas in `xs`.  
`arealist (x:xs) = area x + arealist xs`

- Done!

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