

Types

Since each expression has a type, each definition also has a type.

- `square n = n*n`

then `square` has type `Integer -> Integer`

(Ok, it really is something more generic, but let me lie for once more.)

- `mynumber = square 10`

then `mynumber` has type `Integer`

Specifying Types

- You can specify the type of an expression or a subexpression:

```
10 + 12 :: Integer    --specifies the whole expression
10 + (12 :: Integer) --specifies the 12
```

- You can also specify the type of a definition. Write it on a separate line.

```
square :: Integer -> Integer
square n = n * n
```

- Generally, $x :: T$ is pronounced as “x has type T”.

You may omit such specifications. Then Haskell will compute the most “generic” types possible.

Defining Your Own Types

Let us define a colour type. It will be like an enumerated type.

```
data Colour = Red | Green | Blue
```

- The name of the new type is Colour.
- Its possible values are: Red, Green, Blue.

Note:

- Red, Green, Blue are called *constructors* of Colour: they produce values of the type.
- Type names and constructor names must begin with capital letters.

Writing Functions for Your Types

Let us define a function that maps Colour to integer RGB codes.

Red goes to 255×2^{16} , Green goes to 255×2^8 , Blue goes to 255.

```
toRGB :: Colour -> Int
toRGB c = case c of
  Red -> 255 * 2^16
  Green -> 255 * 2^8
  Blue -> 255
```

This is just like procedural languages. Is there a more elegant way?

Writing Functions for Your Types (cont.)

More elegant way:

```
toRGB :: Colour -> Int
toRGB Red = 255 * 216
toRGB Green = 255 * 28
toRGB Blue = 255
```

Execution view:

- Computer compares the actual parameter with the formal parameters.
- Computer selects the first equation that matches.

This is called *pattern matching*.

How to Write a Function

Human conceptual view:

- I want Red to be mapped to 255×2^{16} .

`toRGB Red = 255 * 2^16`

- I also want Green to be mapped to 255×2^8 .

`toRGB Green = 255 * 2^8`

- I also want Blue to be mapped to 255.

`toRGB Blue = 255`

This is how you should write a function or read one.

More Examples of Functions

More functions written with pattern matching. Try to get used to them.

- Straightforward factorial.

```
factorial :: Integer -> Integer
factorial 1 = 1
factorial n = n * factorial (n-1)
```

- Smart factorial.

```
smartfact :: Integer -> Integer
smartfact n = f 1 n
  where f p 1 = p
        f p i = f (p*i) (i-1)
```

A More Interesting Type

Let us define a shape type. A shape will be a rectangle or an ellipse.

- A rectangle will have a width and a height.
- An ellipse will have a width and a height too (lengths of the axes).

Kind of like a union type.

```
data Shape = Rectangle Float Float
           | Ellipse Float Float
```

Now each constructor takes some parameters.

E.g., `Rectangle` takes two floating-point numbers, a width and a height. (Unfortunately the syntax only lets us write the types.)

A More Interesting Type (cont.)

Some expressions of type Shape:

```
Rectangle 1.0 2.0 :: Shape
```

```
Ellipse 2.0 3.0 :: Shape
```

If you enter them at a Haskell prompt, you'll get an error message:

```
ERROR: Cannot find "show" function for:
```

```
*** Expression : Rectangle 1.0 2.0
```

```
*** Of type    : Shape
```

The computer is saying, "I don't know how to display data of this type."

How do we fix the stupid computer?

A More Interesting Type (cont.)

Add a line “deriving Show” at the end of the type declaration:

```
data Shape = Rectangle Float Float
           | Ellipse Float Float
           deriving Show
```

This tells the computer, “just display data of this type naïvely.”

Now you can enter:

```
Rectangle 1.0 2.0
```

And the computer will display it.

A More Interesting Function

Let us write a function to compute areas of shapes.

```
area :: Shape -> Float
```

- Area of rectangle is width times height.

```
area (Rectangle w h) = w * h
```

The parentheses are needed when there are parameters to the constructor.

- Area of ellipse is π times width times height.

```
area (Ellipse w h) = pi * w * h
```

- Done!

Constructor vs Function

Consider again:

```
Rectangle 1.0 2.0 :: Shape
```

- The constructor is acting like a function:

```
Rectangle :: Float -> Float -> Shape
```

In fact you can use it as such.

- So Red, Green, Blue are like functions requiring no parameters.
- But constructors and functions are different. E.g., cannot use functions in pattern matching.

An Introduction to Lists

Some example lists:

```
[False, True, False] :: [Bool]
[Rectangle 1.0 2.0, Ellipse 2.0 3.0] :: [Shape]
[] --the empty list, pronounced nil
```

- We will discuss the type of [] later. For now, it just works.
- Because of strong typing, Haskell lists are *homogeneous*: all elements in a list must be of the same type.

To simulate heterogenous lists, use list of a union type, just like how we mix rectangles and ellipses in the same list.

An Introduction to Lists (cont.)

- The operator `:` adds an element to the front of a list.

`False:[True]` gives `[False, True]`

- In fact, `[]` and `:` are constructors of the list types.

`[] :: [Bool]`

`(:) :: Bool -> [Bool] -> [Bool]`

So you can use them in pattern matching.

- `[False, True]` is really constructed in these stages:

1. start with constructor `[]`

2. use constructor `:` to add `True`. `True:[]`

3. use constructor `:` to add `False`. `False:True:[]`

A Function Of List

Write a function that adds up a list of integers.

```
addList :: [Integer] -> Integer
```

- Hey I know how to do it when the list is empty.

```
addList [] = 0
```

- If the list is not empty, then it is like $x:xs$, where x is the first number and xs is the rest of the list. I will add x to the sum of xs .

The sum of xs is, of course, `addList xs`.

```
addList (x:xs) = x + addList xs
```

- Done!

A More Interesting Function of List

Write a function that adds up the areas in a list of shapes.

```
areaList :: [Shape] -> Float
```

- Again, I know how to deal with the empty list.

```
areaList [] = 0
```

- If the list is like $x:xs$, I will compute the area of x , then add it to the sum of the areas in xs .

```
areaList (x:xs) = area x + areaList xs
```

- Done!