Guards in Functions

A function to find the "sign" of a number:

```
sgn x = if x>0 then 1 else if x<0 then -1 else
```

Here is a slick way to write it, using guards:

```
sgn x | x>0 = 1
otherwise =
                x<0 = -1
```

Bindings in where clauses are visible in guards:

```
f x | w > 10 = 1
where w = x*x
                   | otherwise = 2
```

Polymorphism

The type of [] is [a]. The a here is called a type variable

upper case.) Note that a type variable begins in lower case. (An actual type begins in

so as to satisfy the context E.g., A type variable can stand for any type. It is instantiated to an actual type

```
Rectangle 1 2 : []
   --a is instantiated to Shape
                             ^{--}a is instantiated to Boolean
```

. Б If the context does not impose any type on a, it remains uninstantiated

--has type [a] when alone

In this way, [] is polymorphic: it can have any of a multitude of types

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Polymorphism

Recall the types of lists:

```
[] :: [what should go here?]
                                    [Rectangle 1 2, Ellipse 1 2] :: [Shape]
                                                                    [True, False] :: [Boolean]
```

Whatever type [] has, it must be consistent with these:

```
Rectangle 1 2 : [] :: [Shape]
                        True : [] :: [Boolean]
```

The first expression requires [] to have type [Boolean].

The second expression requires [] to have type [Shape]

How could this be possible?

Polymorphic Function

A function to count the elements in a list

```
length (x:xs) = 1 + length xs
                    length [] = 0
```

type of the list elements. Its type is [a] -> Integer because nothing in the function determines the

have any of a multitude of types. E.g., This is a polymorphic function: its parameters (and even return values) can

```
length [3, 4] length []
                              length [True, False]
                              --parameter is [Boolean]
                --parameter is
 --parameter is
   а
               [Integer]
```

You can see that polymorphism is Haskell's way of providing genericity.

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Map

Let's say we have a squaring function:

```
square n = n*n
```

and we want to use it to square every element of a list, e.g., if we have a list [1,3,5], we want to get [1,9,25]. We might write:

```
squareList (x:xs) = square x : squareList xs
                                   squareList [] = []
```

Now let's say we have a cube function and we want to do the same:

```
cubeList (x:xs) = cube x : cubeList xs
                             cubeList [] = []
```

This gets boring after a few more examples. Isn't there a better way?

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Higher-Order Functions

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The function

takes a parameter that is in turn a function

In general, functional languages allow a function to take functions as parameters and even return functions as return values. Such a function is called a higher-order function.

One more example: takes a function f and returns a slightly modified function g that does g(x) = f(x) + 1.

```
upOne :: (Int -> Int) -> (Int -> Int)
Where g x = f x + 1
```

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to every element of a list xs, you do this: The Haskell library has a map function. If you want to apply a function f

```
map f xs
```

cubeList: Here is how map looks like; note how it generalizes squareList and

```
\mathsf{map} \ \mathsf{f} \ [] \ = \ []
map f (x:xs) = f x : map f xs
```

may map it to type b. Thus f:=a->b, the input list is [a], and the output list is [b]. Then Let us consider the type of map. An element ${f x}$ may be of type a, and ${f f}$