

314 Let x , y , and n be natural variables. Let $f: \text{nat} \rightarrow \text{nat}$ be a function. Simplify
frame x **new** $y, m: \text{nat} \cdot m := n. x' = f m \wedge y' = f(m+1)$

After trying the question, scroll down to the solution.

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| § | frame x · new $y, m: \text{nat}$ · $m := n$ · $x' = f m \wedge y' = f(m+1)$ | Substitution Law |
| = | frame x · new $y, m: \text{nat}$ · $x' = f n \wedge y' = f(n+1)$ | expand new |
| = | frame x · $\exists y, m, y', m': \text{nat}$ · $x' = f n \wedge y' = f(n+1)$ | discard unused variables |
| = | frame x · $\exists y': \text{nat}$ · $x' = f n \wedge y' = f(n+1)$ | one-point |
| = | frame x · $x' = f n$ | expand frame |
| = | $x' = f n \wedge y' = y \wedge n' = n$ | assignment |
| = | $x := f n$ | |