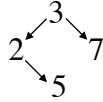


474 An implementer's variable A holds a binary tree representation as follows. If the tree is empty, $A = [nil]$. If the tree has left subtree L and right subtree R and root value n , then $A = [L; n; R]$. The tree



is represented as $A = [[[nil]; 2; [[nil]; 5; [nil]]]; 3; [[nil]; 7; [nil]]]$. The tree must be reimplemented using implementer's variable B as follows. If the tree is empty, $B = 0$. If the tree has left subtree L and right subtree R and root value n , then

$$B = \text{"left"} \rightarrow L \mid \text{"root"} \rightarrow n \mid \text{"right"} \rightarrow R$$

The same example tree is represented as

$$\begin{aligned}
 B = \text{"left"} \rightarrow & \left(\text{"left"} \rightarrow 0 \right. \\
 & \left. \begin{array}{l} \text{"root"} \rightarrow 2 \\ \text{"right"} \rightarrow \left(\text{"left"} \rightarrow 0 \right. \\ \phantom{\text{"right"} \rightarrow} \left. \begin{array}{l} \text{"root"} \rightarrow 5 \\ \text{"right"} \rightarrow 0 \end{array} \right) \end{array} \right) \\
 & \left. \begin{array}{l} \text{"root"} \rightarrow 3 \\ \text{"right"} \rightarrow \left(\text{"left"} \rightarrow 0 \right. \\ \phantom{\text{"right"} \rightarrow} \left. \begin{array}{l} \text{"root"} \rightarrow 7 \\ \text{"right"} \rightarrow 0 \end{array} \right) \end{array} \right)
 \end{aligned}$$

- (a) What is the data transformer?
 (b) A user has natural variable n and the operation

$$root = n := A \ 1$$

which assigns to n the root value. Use your transformer from part (a) to transform $root$.

no solution given